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Special Publication No. 171

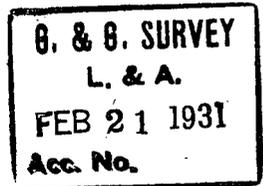
## WORLD LONGITUDE DETERMINATIONS BY THE UNITED STATES COAST AND GEODETIC SURVEY IN 1926

BY

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QB  
275  
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no. 171  
1931



UNITED STATES  
GOVERNMENT PRINTING OFFICE  
WASHINGTON : 1931

# National Oceanic and Atmospheric Administration

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# WORLD LONGITUDE DETERMINATIONS BY UNITED STATES COAST AND GEODETIC SURVEY IN 1926

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## ABSTRACT

During the autumn of 1926, a world-wide program of longitude determinations by a number of countries was carried out under the direction of a mixed commission of the International Astronomical Union and the International Geodetic and Geophysical Union. The chairman of this commission is Gen. G. Ferrié, of France. The stations were divided into two groups, a fundamental polygon of three stations encircling the globe and a number of secondary stations connected to this polygon.

Four of the stations were in United States territory. The observations at two of these stations, one at Niu, about 7 miles southeast of Honolulu, and the other at Fort Wm. McKinley, about 6 miles southeast of Manila, were made by the Coast and Geodetic Survey.

Recently a French publication<sup>1</sup> was issued, giving the final differences for the fundamental polygon, Algiers, Zikawei, and San Diego. With these data available, it seemed advisable for this bureau to publish the results for its two stations and to give the final differences of longitude from two of the fundamental stations, Zikawei and San Diego. For the convenience of those who wish to make a detailed study of all the results of the world longitude program, the data are here published in practically the same form as in Lambert's book, mentioned above.

The final adjusted longitudes of Niu and Fort Wm. McKinley, based on the final published longitudes of Zikawei and San Diego, are as follows:

**Longitude of Niu =  $10^{\text{h}} 30^{\text{m}} 55^{\text{s}}.282$  west of Greenwich; longitude of Fort Wm. McKinley =  $8^{\text{h}} 04^{\text{m}} 12^{\text{s}}.641$  east of Greenwich.**

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## INCEPTION OF WORLD LONGITUDE NET

At the meeting in Rome, in 1922, of the International Astronomical Union and the International Geodetic and Geophysical Union, it was proposed by the Bureau of Longitudes, on the initiative of Gen. G. Ferrié, to establish a world-wide network of longitude stations with differences of longitude determined simultaneously at the various stations. It was proposed to make use of radio signals from a few powerful radio stations as the means for comparing the local times at the different stations, and it was planned to make the local time determinations with some standard high-grade instrumental equipment.

A mixed commission of the two international unions with General Ferrié as chairman, was appointed at the Rome meeting to perfect plans for this project. At the Madrid meeting of the International Geodetic and Geophysical Union, in 1924, and at the meeting in Cambridge, in 1925, of the International Astronomical Union, a definite plan for the work was finally agreed upon, and it was decided to make the observations in October and November of 1926. According to this plan the stations of the net were divided into two groups, a fundamental polygon of three stations, Algiers, San Diego, and Zikawei, encircling the globe, and in the second group a number of secondary stations connected to the fundamental stations.

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<sup>1</sup> Lambert, Armand, *la Participation Française à la Révision des Longitudes Mondiales*, Toulouse, 1928.

The observations at two of the secondary stations were undertaken by the Coast and Geodetic Survey. In the preliminary list of stations prepared by the commission these two stations were designated as Honolulu and Manila, at both of which places there were old longitude stations determined by the cable and wire-telegraph method. At both places, however, it was necessary to locate the new stations at some distance away from the old stations, in order to secure satisfactory conditions for the reception of the radio signals. At Honolulu the new station is on the coast, about 7 miles southeast of the city, at a place called Niu. At Manila the new station is about 6 miles southeast of the city, on the Government reservation at Fort Wm. McKinley. Both of the new stations were connected with the old cable stations by determining the differences of longitude astronomically.

The work at Niu was under the direction of Lieut. E. J. Brown who was assisted by Lieut. W. H. Bainbridge, and at Fort Wm. McKinley it was under the direction of Lieut. R. J. Sipe who was assisted by Ensign F. G. Bryan and by J. I. Edwards, wireless operator. These men deserve a great deal of credit for the successful completion of the observations in spite of formidable difficulties and with instrumental equipment much less elaborate than at many of the other stations of the net, several of which were at astronomical observatories. The preliminary field computations were made by Lieutenants Brown, Bainbridge, and Sipe. In making the office computations, the writer was assisted by Associate Mathematician F. W. Darling and Assistant Mathematician J. A. Duerksen, who also helped in preparing the manuscript of this publication.

In 1927 this bureau issued, in mimeograph form, the preliminary results at stations Niu and Fort Wm. McKinley. Before the final results could be computed, it was necessary to know the final adopted differences for the three stations of the principal world polygon—Algiers, San Diego, and Zikawei. These differences are now available in published form in a French report by Armand Lambert.<sup>2</sup> It seemed advisable at this time, therefore, to compute and publish the final differences for the two stations determined by this bureau. The results are here given as nearly as possible in the same form as in Lambert's publication. There are two reasons for this: It seemed impossible to improve on the general arrangement adopted by Lambert, and it was felt that a study of the results for the complete network of stations could be made more conveniently if all the data were published according to a standard form.

In preliminary discussions in regard to making the final adjustments for the various secondary stations, it was thought that the stations should be combined in two comprehensive nets, one for the Pacific area and another for the rest of the world. Informal plans were made for the Coast and Geodetic Survey to have charge of the Pacific adjustment. After considerable study of the matter, and after the experience gained in making the adjustment of its own two stations, this bureau finds it advisable to recommend that each organization in the Pacific area which took part in the world longitude work make the adjustment of its own stations.

Apparently nothing is to be gained by connecting a secondary station to a large number of other secondary stations, although

<sup>2</sup> See footnote 1 on p. 1.

the small number of signals received at Fort Wm. McKinley made it desirable to connect this station in the adjustment with Niu (which, of course, is a secondary station) as well as with the principal stations of San Diego and Zikawei. Ordinarily, however, a secondary station can be connected with main polygon stations only, and the results should be as accurate as if it were connected also with several secondary stations. It is also true that each organization that made observations for the world longitude net is in a much better position to interpret its own observations and assign the proper weights, etc., than is any central office which might undertake the work.

### METHODS AND APPARATUS

At each station a Bamberg broken-telescope transit equipped with a hand-driven transit micrometer was used for making the time observations, and the common practice of this bureau of observing time stars only, instead of part time and part azimuth stars, was employed.<sup>3</sup> The radio equipment consisted primarily of the long-wave radio-recording device, described in Special Publication No. 109, which has been used so successfully by this bureau for several years for longitude and gravity determinations. A short-wave receiver, constructed in the field, was also used at each station, and although it proved quite satisfactory for receiving the signals, it did not give satisfactory results because of an unexpectedly large and variable lag which could not be correctly evaluated.

One of the serious problems which confronted this bureau when plans were being made for the work was how to provide accurate timepieces in order to compare the time derived from the astronomical observations with the time of the radio signals, which were received at various times of day and night, often at intervals of several hours from the mean epoch of the astronomical determinations. Chronometers were not accurate enough for the purpose, and no Riefler or other astronomical clocks were available. Even if astronomical clocks had been available, it would have been impracticable to construct constant-temperature vaults and make the elaborate preparations necessary for their installation at these two field stations.

The problem was solved by Doctor Bowie, who suggested the use of a gravity pendulum as a precision timepiece.<sup>4</sup> The quarter-meter, half-second pendulum used in the gravity apparatus of the Coast and Geodetic Survey is a free-swinging pendulum of the invariable type. It is swung in an air-tight receiver in a partial vacuum. If the temperature and pressure conditions are kept fairly uniform and corrections are applied for decrease in amplitude, the pendulum will maintain a very constant rate, and for intervals of a few hours it constitutes a timepiece which is probably as accurate as any timepiece in existence at the present time.

The method of using the pendulum to meet the special requirements of the longitude work was as follows: The period of the pendulum was first carefully determined at the station in the manner usually employed

<sup>3</sup> A description of the Bamberg broken-telescope transit and a detailed explanation of its use for time determinations will be found in U. S. Coast and Geodetic Survey Special Publication No. 35. The older methods employed by this bureau for its longitude determinations are described in Special Publication No. 14. The radio method is explained in Special Publication No. 109.

<sup>4</sup> See William Bowie, Use of the Gravity Pendulum as a Timepiece, U. S. Coast and Geodetic Survey Serial No. 356, Washington, 1926.

at a field gravity station.<sup>5</sup> The pendulum was then used to check the rate of the chronometer over the interval between the mean epoch of the time observations and the time of the radio signal. The comparison between the chronometer and the swinging pendulum was made by the method of coincidences, as in gravity determinations.

The time could be carried over an interval of 12 hours in this manner with very little loss in accuracy. This was proved in several cases by comparing a given radio signal which happened to come

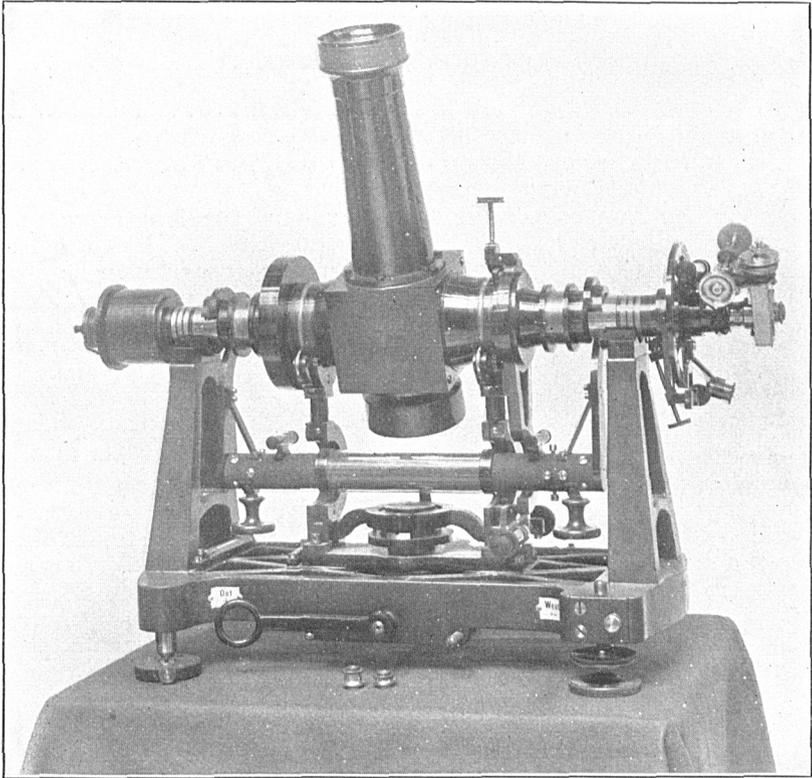


FIGURE 1.—BAMBERG BROKEN-TELESCOPE TRANSIT

This type of instrument was used for making the local time observations at both Niu and Fort Wm. McKinley.

about midway between the mean epochs of the time observations on succeeding nights with each of the two time determinations. The results of the two comparisons agreed within one or two hundredths of a second in most cases.

The pendulum was kept swinging almost continuously at Niu during the two months of longitude observations, and many of the radio signals, which could not have been used otherwise, were thus connected with the local time observations. At Fort Wm. McKinley the observer did not attempt to use the pendulum as a timepiece, as he was able to make star observations near the time of all signals that he was

<sup>5</sup> See Clarence H. Swick, *Modern Methods for Determining the Intensity of Gravity*, U. S. Coast and Geodetic Survey Special Publication No. 69, Washington, 1921.

able to receive. He did, however, make a determination of gravity at the station by swinging the pendulums for several days.

In the following tables it will be noticed that the number of determinations at Fort Wm. McKinley is rather small. This was due to

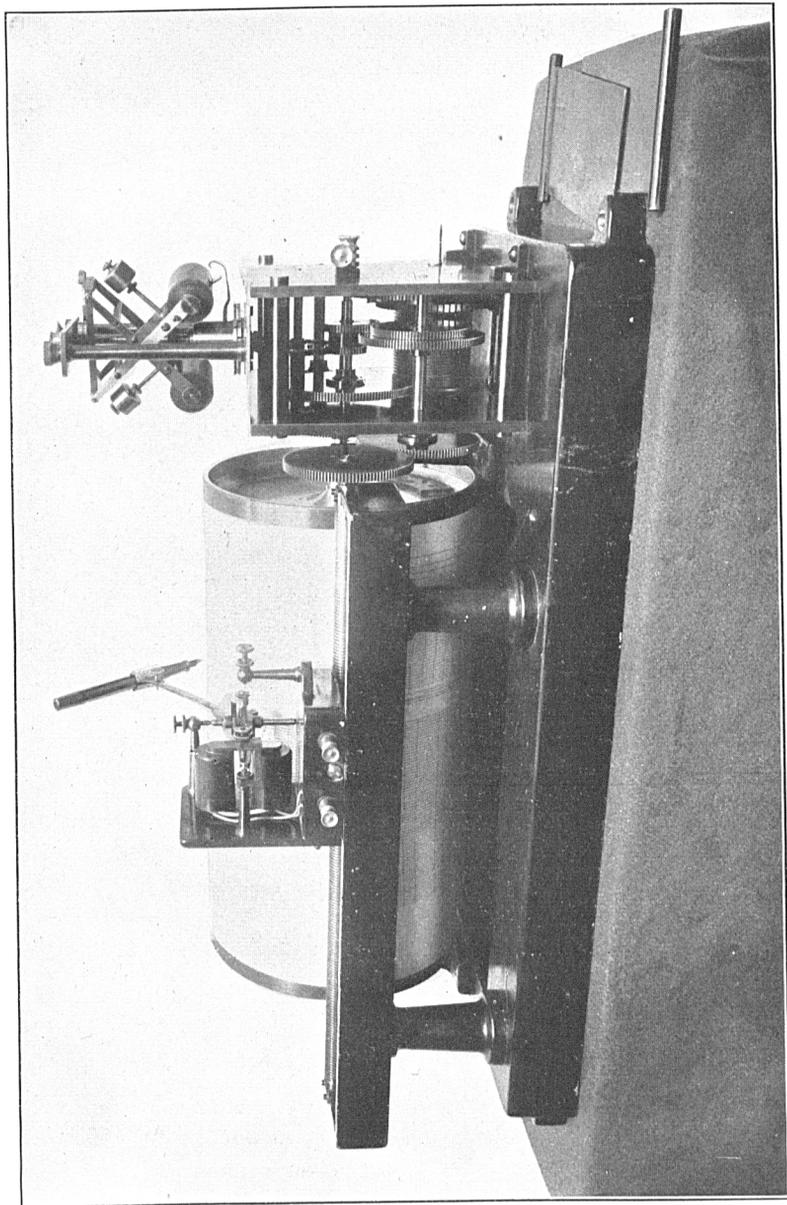


FIGURE 2.—CHRONOGRAPH  
The radio time signals and the transit star observations were recorded on this type of chronograph at both stations.

several causes. The observer was unavoidably late in reaching his station and did not have time enough to get his instruments and apparatus in working order before the 1st of October, when the work was supposed to start. His chief difficulty was with the radio appa-

ratus, for although this apparatus was in good condition when it left Washington, the long shipment and bad climatic conditions had ruined several of the parts by the time attempts were made to use it in the field. A great deal of rewiring had to be done, not only on

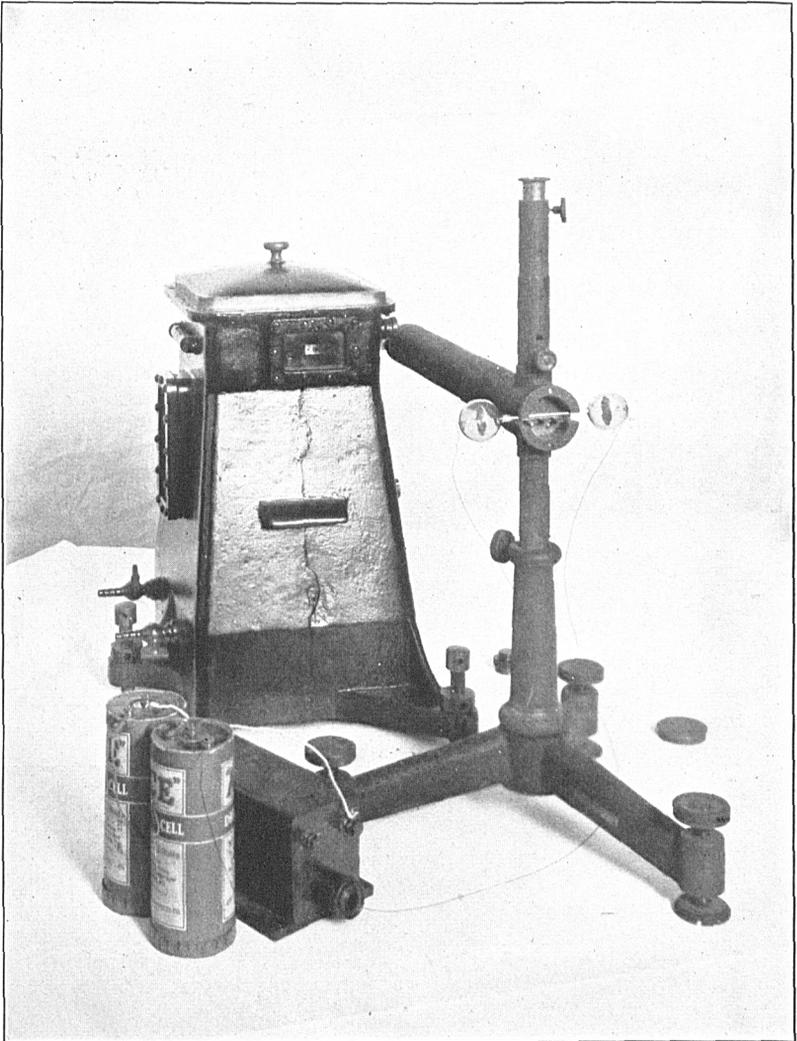


FIGURE 3.—GRAVITY RECEIVER AND INTERFEROMETER

The gravity pendulum was used in place of a precise clock at station Niu. As at an ordinary gravity station, the pendulum was swung under a partial vacuum in the receiver shown here. The interferometer was used to determine the slight sway of the receiver caused by the oscillations of the pendulum in order that a correction could be applied for the flexure.

the radio set but on the chronograph, longitude switchboard, and other parts of the instrumental equipment.

In his report on the work, Lieutenant Sipe makes grateful acknowledgment to various ones for the assistance he received in making repairs to his apparatus, in erecting his observatory, and in making other preparations for the work. He mentions especially Lieutenant

Paddock, who was in charge of the Santiago radio station, and Mr. Eason, a radio engineer at the Cavite Navy Yard.

For the work at Niu, Lieutenant Brown, in his report, mentions the valuable cooperation and assistance of Surveyor General Wall,

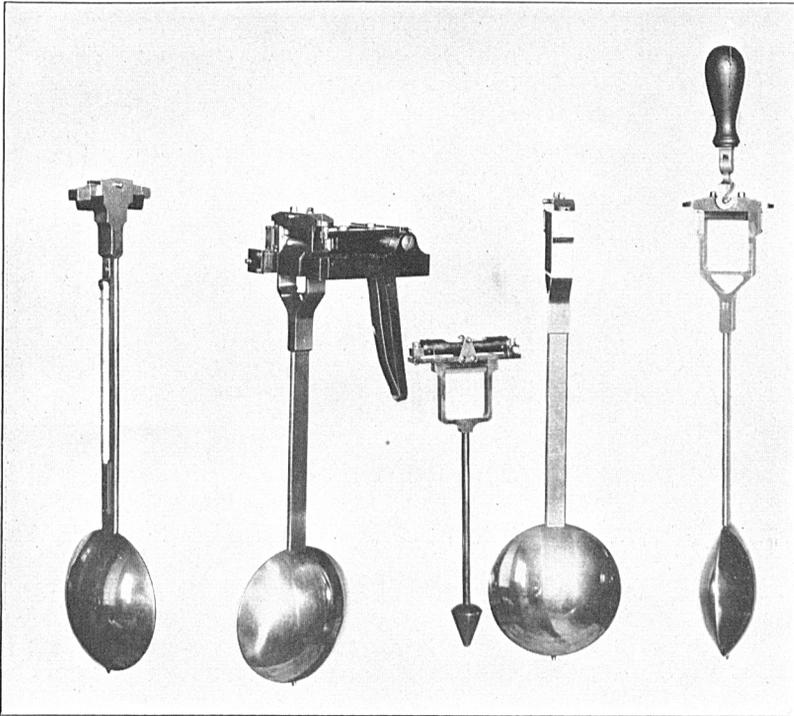


FIGURE 4.—GRAVITY PENDULUMS

The pendulum to the left is called the dummy. It carries the thermometer but is not permitted to swing. The pendulum in the center has a level mounted on it which is used to level the knife edge. The three others shown are the gravity pendulums. The one to the left of the center is supported on the knife edge.

Admiral McDonald and the radio division of the Navy, and the technical staff of the Radio Corporation of America.

SIGNALS

The following table contains a list of the signals received at Niu and Fort Wm. McKinley, showing the Greenwich civil times at which the signals were emitted, the wave lengths, and other data.

*Signals received at Niu and Fort Wm. McKinley*

Reference number of signal	Greenwich civil time of signal	Wave length of signal	Radio station emitting	Type of signal
		<i>Meters</i>		
3.....	3. 20- 3. 25	25	Bellevue.....	Rhythmic.
4.....	3. 20- 3. 25	75	.....do.....	Do.
5.....	3. 30- 3. 35	11, 500	Honolulu.....	Do.
6.....	3. 40- 3. 45	37	.....do.....	Do.
15.....	10. 20-10. 25	75	Bellevue.....	Do.
16.....	10. 30-10. 35	11, 500	Honolulu.....	Do.
17.....	10. 40-10. 45	37	.....do.....	Do.
19.....	11. 30-11. 35	15, 800	Saigon.....	Do.
23.....	19. 00-19. 05	15, 800	.....do.....	Do.
31.....	20. 30-20. 35	11, 500	Honolulu.....	Do.
32.....	20. 40-20. 45	37	.....do.....	Do.

The beat interval of all the above signals was about 60/61 mean time second. Saigon sent 300 beats for each signal and the rest of the stations 306 beats, although occasionally a few extra beats were sent at the end of the signal. Identification of the beats was assured in



FIGURE 5.—OBSERVATORY AND ANTENNA AT NIUE (NEAR HONOLULU)

The far end of the antenna was supported by a pole which stood on the rocky knob in the left background.

the following manner. The 60th, 120th, 180th, 240th, and 300th beats of the Honolulu signals were omitted; the 1st, 62d, 123d, 184th, 245th, and 306th beats of the Bellevue signals were elongated; the 60th, 120th, 180th, and 240th beats of the Saigon signals were elon-

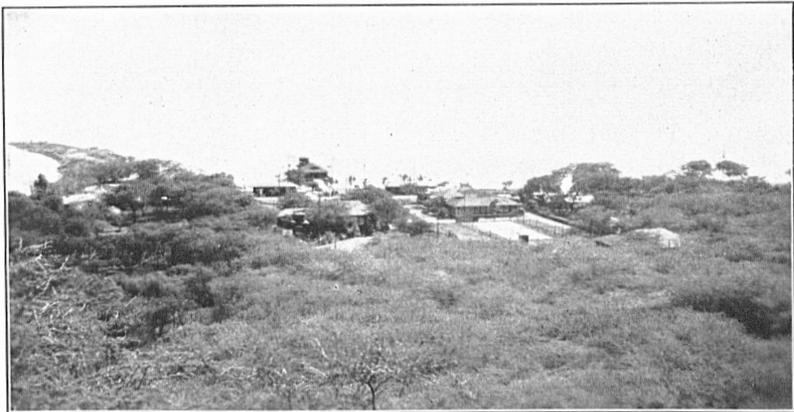


FIGURE 6.—U. S. NAVY RADIO STATION AT WAILUPE

The Honolulu signals were controlled from this station which is only about 2 miles from Niue.

gated. The Saigon signals were subject to a large and variable rate, and the factor for reducing each beat to the last or 300th beat was obtained from the internal evidence within the series of beats.

Although the sending clock at Honolulu had a very much smaller rate than the clock at Saigon, this rate was taken into account in

computing the reduction factor used in reducing each beat read from the chronograph sheet to the final or 306th beat and in computing the first beat of each Honolulu signal from the derived time of the 306th.

The Bellevue signals were controlled by the Naval Observatory clock and so no rate correction was required.

Two of the following tables, one for Niu and one for Fort Wm. McKinley (see pp. 11-13 and 21), give the local sidereal times of the reception of both the first and last beats of each radio signal. The two beats are not independently determined. The time of the last beat of each signal was first derived and the time of the first beat was then computed from that. For the Bellevue signals the interval between the first and last beat was 300<sup>s</sup>.821. For the Honolulu signals the interval varied from 300<sup>s</sup>.805 to 300<sup>s</sup>.809 and for the Saigon signals it varied from 294<sup>s</sup>.515 to 294<sup>s</sup>.688. The interval for the Saigon signals may in some cases be in error by as much as several hundredths of a second as static interference made some of the Saigon chronograph sheets very difficult to read.

#### LAGS

The transit-circuit lag of Bamberg transit No. 20 and longitude switchboard No. 2, the radio receiver lags of the long-wave and short-wave sets used at Niu, and the personal equation of the Niu observer were determined in Washington. The total correction for lag amounted to +0<sup>s</sup>.030 when the long-wave set was used, and +0<sup>s</sup>.023 when the short-wave set was used. These corrections were applied to all observations at Niu and also to those at Fort Wm. McKinley.

In deriving preliminary longitude differences between Niu and Washington and between Niu and San Diego, by comparing the reception times of the various signals with the reception times at Washington and San Diego, it was discovered that there was a fairly consistent discrepancy of about 0<sup>s</sup>.07 between the results derived from the short-wave signals and those derived from the long-wave signals. This was undoubtedly due mostly to an uncorrected lag in the short-wave receiver at Niu. As the Naval Observatory observers were able to make very careful determinations of the lags of their short-wave receivers in the field, and as this bureau's observer was unable to do this, it was decided to attribute the entire discrepancy to a lag in the Niu short-wave receiver. All times for signals Nos. 3, 4, 6, 15, 17, and 32 at Niu have therefore been decreased by 0<sup>s</sup>.07. At Fort Wm. McKinley a comparison of the reception times with those at Niu, San Diego, and Washington seemed to show an uncorrected lag of 0<sup>s</sup>.02 in the short-wave receiver. All times for signal No. 17 at this station have therefore been decreased by this amount. It is recommended that other stations comparing their reception times with those of this bureau use only the long-wave signals unless this gives an inadequate number of comparisons. The data given in this publication for the short-wave signals should be used with caution. No short-wave signals were used in computing the longitudes of Niu and Fort Wm. McKinley.

#### TRANSMISSION TIMES

Corrections for the interval of time required for the signals to travel from the radio transmitting station to the receiving station were not

applied in deriving the signal times listed in the two tables on pages 11-13 and 21. These tables therefore give the local sidereal times at the respective receiving stations for the instants at which the first and last beats of each radio signal were received at these stations. Transmission times were taken into account only in computing the differences of longitude between stations, as shown in the tables on pages 17 and 24. The computations of the transmission-time corrections are shown on pages 17 and 23. The velocity of propagation of radio

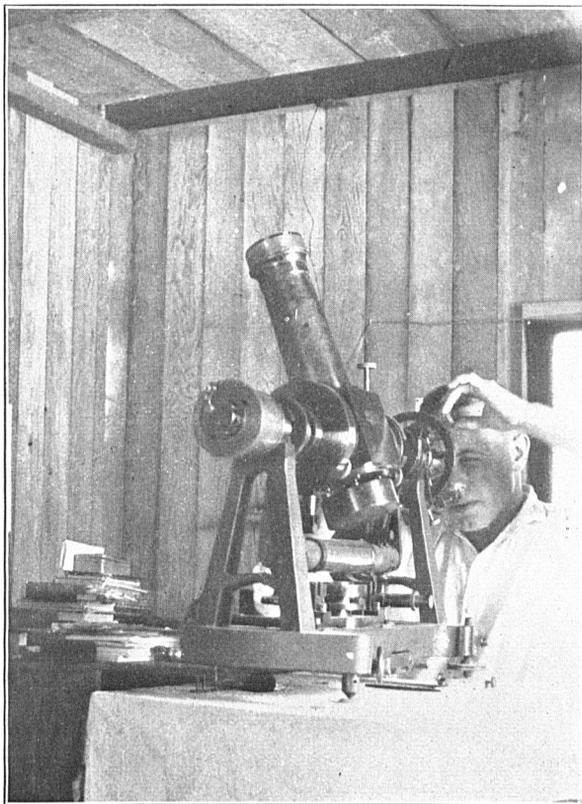


FIGURE 7.—MAKING STAR OBSERVATIONS AT NIU

The local sidereal time was determined on every clear night during the two months of the international program.

waves was assumed to be equal to the velocity of light, or approximately 300,000 kilometers per second.

#### RESULTS AT STATION NIU (near Honolulu)

##### DESCRIPTION OF STATION

Station Niu is about 7 miles southeast of Honolulu, Island of Oahu, Hawaii, at Niu, on the Chas. Lucas dairy ranch, 4 meters north of the stone wall on the north side of the road and about 100 meters west of the Lucas residence. The station is marked by a standard disk triangulation station mark of the U. S. Coast and Geodetic Survey set in concrete, stamped "Niu longitude 1926."

*Local sidereal times of reception of radio signals*

SIGNALS FROM BELLEVUE, NO. 3 (3.20-3.25; 25 METERS)<sup>1</sup>

Date, 1926	Local sidereal time					
	Beat No. 1			Beat No. 306		
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 20.....	18	40	24.413	18	45	25.234

SIGNALS FROM BELLEVUE, NO. 4 (3.20-3.25; 75 METERS)<sup>1</sup>

Nov. 24.....	20	58	23.905	21	03	24.726
Nov. 27.....	21	10	13.594	21	15	14.415
Nov. 28.....	14	10	10.157	19	10	10.978

SIGNALS FROM HONOLULU, NO. 5 (3.30-3.35; 11,500 METERS)

Date, 1926	Local sidereal time						Date, 1926	Local sidereal time					
	Beat No. 1			Beat No. 306				Beat No. 1			Beat No. 306		
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>		<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 12.....	18	19	30.710	18	24	31.516	Nov. 5.....	19	54	32.062	19	59	32.870
Oct. 13.....	23	22	22.910	28	23	23.716	Nov. 7.....	20	01	18.815	20	06	19.624
Oct. 14.....	27	15	15.337	32	16	16.143	Nov. 9.....	10	03	03.570	15	04	03.799
Oct. 15.....	31	07	07.786	36	08	08.592	Nov. 10.....	13	56	30.505	18	57	11.114
Oct. 19.....	46	37	37.533	51	38	38.340	Nov. 11.....	17	49	23.211	22	50	00.040
Oct. 20.....	50	30	30.058	55	30	30.865	Nov. 15.....	32	21	24.737	37	22	05.660
Oct. 22.....	59	14	14.440	19	04	15.247	Nov. 18.....	44	59	80.111	50	00	00.610
Oct. 26.....	19	14	44.550	19	45	45.357	Nov. 19.....	48	52	93.888	53	53	74.777
Oct. 27.....	20	35	35.515	25	36	36.322	Nov. 24.....	21	09	18.563	21	14	19.372
Oct. 29.....	26	22	22.621	31	23	23.429	Nov. 25.....	12	12	55.555	17	13	36.364
Oct. 30.....	30	15	15.600	35	16	16.408	Nov. 27.....	20	57	80.909	25	58	61.818
Nov. 2.....	19	41	53.945	19	46	54.753	Nov. 28.....	24	51	04.729	29	51	85.666
Nov. 3.....	45	46	46.805	50	47	47.613	Nov. 30.....	32	36	97.979	37	37	78.888
Nov. 4.....	49	39	78.555	54	40	59.333	Dec. 1.....	21	36	29.973	21	41	30.782

SIGNALS FROM HONOLULU, NO. 6 (3.40-3.45; 37 METERS)<sup>1</sup>

Oct. 19.....	18	57	28.456	19	02	29.263	Nov. 10.....	20	23	48.126	20	28	48.935
Oct. 26.....	19	24	36.343	29	37	37.150	Nov. 11.....	27	41	04.333	32	41	85.222
Oct. 27.....	28	28	28.957	33	29	29.764	Nov. 15.....	42	13	06.666	47	13	87.555
Oct. 29.....	36	14	39.333	41	15	20.111	Nov. 19.....	58	44	72.929	21	03	45.538
Oct. 30.....	40	07	40.833	45	08	21.111	Nov. 24.....	21	17	12.033	22	12	84.222
Nov. 2.....	19	51	45.722	19	56	46.529	Nov. 25.....	22	04	37.888	27	05	18.777
Nov. 3.....	55	38	60.666	20	00	39.413	Nov. 27.....	30	49	61.666	35	50	42.555
Nov. 4.....	20	00	30.703	05	31	51.111	Nov. 28.....	34	42	85.111	39	43	66.000
Nov. 5.....	04	23	80.833	09	24	61.111	Nov. 30.....	42	28	77.333	47	29	58.222
Nov. 7.....	12	09	72.929	17	10	53.888	Dec. 1.....	21	46	21.788	21	51	22.597

SIGNALS FROM BELLEVUE, NO. 15 (10.20-10.25; 75 METERS)<sup>1</sup>

Nov. 9.....	3	00	24.591	3	05	25.412	Nov. 23.....	3	55	36.390	4	00	37.211
Nov. 10.....	04	21	15.919	09	21	98.000	Nov. 25.....	4	03	29.484	08	30	30.305
Nov. 11.....	08	17	69.777	13	18	51.818	Nov. 27.....	11	22	55.555	16	23	37.666
Nov. 13.....	16	10	76.333	21	11	58.444	Nov. 30.....	23	12	33.888	28	13	15.919
Nov. 19.....	39	50	15.666	44	50	97.777							

<sup>1</sup> These short-wave signals were not used in computing the longitude of Niue. See p. 9.

*Local sidereal times of reception of radio signals—Continued*

## SIGNALS FROM HONOLULU, NO. 16 (10.30-10.35; 11,500 METERS)

Date, 1926	Local sidereal time						Date, 1926	Local sidereal time					
	Beat No. 1			Beat No. 306				Beat No. 1			Beat No. 306		
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>		<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 8.....	1	04	10.138	1	09	10.943	Nov. 8.....	3	07	18.762	3	12	19.571
Oct. 11.....		15	47.092		20	47.898	Nov. 9.....		10	12.230		15	13.039
Oct. 12.....		20	38.475		25	39.281	Nov. 10.....		15	04.286		20	05.095
Oct. 14.....		28	23.192		33	23.998	Nov. 11.....		18	57.180		23	57.989
Oct. 15.....		32	15.534		37	16.340	Nov. 13.....		25	43.538		30	44.347
Oct. 19.....		47	45.350		52	46.157	Nov. 15.....		34	28.483		39	29.292
Oct. 20.....		51	37.896		56	38.703	Nov. 18.....		46	07.866		51	08.675
Oct. 26.....	2	15	52.422	2	20	53.229	Nov. 19.....		50	00.973		55	01.782
Oct. 27.....		19	45.016		24	45.823	Nov. 23.....	4	05	34.123	4	10	34.932
Oct. 29.....		27	30.584		32	31.392	Nov. 24.....		10	26.629		15	27.438
Oct. 30.....		31	23.544		36	24.352	Nov. 25.....		13	20.563		18	21.372
Nov. 2.....	2	43	01.899	2	48	02.707	Nov. 27.....		21	06.658		26	07.467
Nov. 3.....		46	54.766		51	55.574	Nov. 28.....		25	58.722		30	59.781
Nov. 4.....		50	47.785		55	48.593	Nov. 29.....		29	51.983		34	52.792
Nov. 5.....		54	40.898		59	41.706	Nov. 30.....		33	44.971		38	45.780
Nov. 7.....	3	03	25.949	3	08	26.758							

SIGNALS FROM HONOLULU, NO. 17 (10.40-10.45; 37 METERS)<sup>1</sup>

Oct. 20.....	2	01	29.688	2	06	30.495	Nov. 15.....	3	44	20.287	3	49	21.096
Oct. 26.....		25	44.189		30	44.996	Nov. 18.....		55	59.673	4	01	00.482
Oct. 29.....		37	22.362		42	23.170	Nov. 19.....		59	52.762		04	53.571
Oct. 30.....		41	15.312		46	16.120	Nov. 24.....	4	20	18.406		25	19.215
Nov. 2.....	2	52	53.688	2	57	54.496	Nov. 25.....		23	12.377		28	13.186
Nov. 5.....	3	04	32.636	3	09	33.444	Nov. 27.....		30	58.436		35	59.245
Nov. 8.....		17	10.505		22	11.314	Nov. 28.....		35	50.757		40	51.566
Nov. 9.....		21	03.203		26	04.012	Nov. 29.....		39	43.791		44	44.600
Nov. 11.....		28	48.984		33	49.793	Nov. 30.....		43	36.789		48	37.598
Nov. 13.....		36	34.498		41	35.307							

## SIGNALS FROM SAIGON, NO. 19 (11.30-11.35; 15,800 METERS)

Date, 1926	Local sidereal time						Date, 1926	Local sidereal time					
	Beat No. 1			Beat No. 300				Beat No. 1			Beat No. 300		
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>		<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 30.....	3	29	18.715	3	34	13.344	Nov. 15.....	4	34	06.942	4	39	01.630
Nov. 3.....	3	44	05.706	3	49	00.329	Nov. 18.....		44	46.436		49	41.026
Nov. 8.....	4	02	25.673	4	07	20.203	Nov. 23.....	5	04	15.745	5	09	10.353
Nov. 9.....		08	03.557		12	58.123	Nov. 25.....		12	41.214		17	35.798
Nov. 13.....		22	46.112		27	40.657							

## SIGNALS FROM SAIGON, NO. 23 (19.00-19.05; 15,800 METERS)

Nov. 18.....	12	16	02.955	12	20	57.572	Nov. 23.....	12	34	46.143	12	39	40.670
Nov. 19.....		20	06.086		25	00.709							

<sup>1</sup> These short-wave signals were not used in computing the longitude of Niu. See p. 9.

Local sidereal times of reception of radio signals—Continued

SIGNALS FROM HONOLULU, NO. 31 (20.30-20.35; 11,500 METERS)

Date, 1926	Local sidereal time						Date, 1926	Local sidereal time					
	Beat No. 1			Beat No. 306				Beat No. 1			Beat No. 306		
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>		<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 11.....	11	18	23.038	11	23	23.844	Nov. 7.....	13	05	03.072	13	10	03.881
Oct. 12.....		22	15.265		27	16.071	Nov. 8.....		08	55.704	13	56	51.3
Oct. 13.....		26	07.646		31	08.452	Nov. 9.....		12	48.492	17	49	30.1
Oct. 14.....		30	00.041		35	00.847	Nov. 10.....		16	41.435	21	42	24.4
Oct. 15.....		33	52.368		38	53.174	Nov. 11.....		20	34.180	25	34	98.9
Oct. 18.....		45	29.791		50	30.598	Nov. 12.....		24	26.946	29	27	75.5
Oct. 19.....		49	22.218		54	23.025	Nov. 13.....		28	19.737	33	20	54.6
Oct. 20.....		53	14.838		58	15.645	Nov. 14.....		32	12.446	37	13	25.5
Oct. 21.....		57	07.449	12	02	08.256	Nov. 15.....		36	05.687	41	06	49.6
Oct. 22.....	12	01	00.184		06	00.991	Nov. 17.....		43	51.875	48	22	68.4
Oct. 25.....		13	36.805		18	37.612	Nov. 23.....	14	08	10.601	14	13	11.410
Oct. 26.....		17	29.326		22	30.133	Nov. 24.....		12	03.790	17	04	59.9
Oct. 27.....		21	21.918		26	22.725	Nov. 25.....		15	56.820	20	57	62.9
Oct. 28.....		25	14.704		30	15.511	Nov. 26.....		19	49.812	24	50	62.1
Oct. 29.....		29	07.682		34	08.490	Nov. 27.....		23	42.846	28	43	65.5
Nov. 1.....	12	40	46.097	12	45	46.905	Nov. 28.....		27	36.049	32	36	85.8
Nov. 2.....		44	38.904		49	39.712	Nov. 29.....		31	29.031	36	29	84.0
Nov. 3.....		48	31.847		53	32.655	Nov. 30.....		35	22.018	40	22	82.7
Nov. 4.....		52	24.856		57	25.664							
Nov. 6.....	13	01	10.162	13	06	10.970							

SIGNALS FROM HONOLULU, NO. 32 (20.40-20.45; 37 METERS)<sup>1</sup>

Oct. 15.....	11	43	44.110	11	48	44.916	Nov. 9.....	13	22	40.299	13	27	41.108
Oct. 18.....		55	21.532	12	00	22.339	Nov. 11.....		30	25.995	35	26	80.4
Oct. 19.....		59	13.931		04	14.738	Nov. 12.....		35	18.774	40	19	58.3
Oct. 20.....	12	03	06.637		08	07.444	Nov. 13.....		38	11.552	43	12	36.1
Oct. 21.....		06	59.250		12	00.057	Nov. 14.....		42	04.245	47	05	05.4
Oct. 22.....							Nov. 15.....		45	57.490	50	58	29.9
Oct. 25.....		11	51.147		16	51.954	Nov. 17.....		53	43.660	58	44	46.9
Oct. 26.....		23	28.506		28	29.313	Nov. 19.....	14	01	29.973	14	06	30.782
Oct. 28.....		35	06.471		40	07.278	Nov. 23.....		18	02.411	23	03	22.0
Oct. 29.....		38	59.466		44	00.274	Nov. 24.....		21	55.587	26	56	39.6
Nov. 1.....	12	50	37.900	12	55	38.708	Nov. 25.....		25	48.628	30	49	43.7
Nov. 3.....		58	23.583	13	03	24.391	Nov. 26.....		29	41.604	34	42	41.3
Nov. 4.....	13	02	16.605		07	17.413	Nov. 27.....		33	34.671	38	35	48.0
Nov. 6.....		11	01.903		16	02.711	Nov. 28.....		37	27.873	42	28	68.2
Nov. 7.....		14	54.788		19	55.597	Nov. 29.....		41	20.837	46	21	64.6
Nov. 8.....		18	47.464		23	48.273	Nov. 30.....		45	13.825	50	14	63.4

<sup>1</sup> These short-wave signals were not used in computing the longitude of Niu. See p. 9.

COMPUTATION OF LONGITUDE, STATION NIU

The following tables and the least-squares adjustment on pages 17 and 18 show how the longitude of Niu was obtained. The first table gives the local sidereal times at which Honolulu signal No. 16 was received by Niu and Zikawei on the different days on which that signal was received by both stations. The differences of these local times, shown in the last column of the table, are preliminary, uncorrected values of the difference in longitude between the two stations, Niu and Zikawei. The mean of these differences is given a weight equal to the number of accepted values used in obtaining it. The criterion for making rejections of outstanding differences is explained in the footnote on page 14.

Following this table are similar tables for the other signals received by both Niu and Zikawei and also for the signals received by both Niu and San Diego.

The next table shows the computation of the corrections for transmission times. These corrections are applied in the next following table to the mean differences of longitude as derived from the various sets of signals. Weighted means are then taken to give the corrected differences of longitude between Niu and each of the two fundamental stations, Zikawei and San Diego.

The final step in the computation is the least-squares adjustment to obtain corrections to the two differences of longitude to make them sum up to the fixed difference between San Diego and Zikawei. This adjustment is very simple and requires no explanation. It is given in complete detail on pages 17 and 18.

*Comparison of local sidereal times at Niu and Zikawei*

HONOLULU SIGNALS NO. 16

Date, 1926	Sidereal time of 306th beat						Difference, Niu minus Zikawei		
	Niu			Zikawei <sup>1</sup>					
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 8.....	1	09	10.943	19	45	49.11	5	23	21.833
Oct. 12.....	1	25	39.281	20	02	30.36			08.921 R <sup>2</sup>
Oct. 14.....	1	33	23.998	20	10	02.12			21.878 R <sup>2</sup>
Oct. 19.....	1	52	46.157	20	29	24.37			21.787
Oct. 20.....	1	56	38.703	20	34	16.15			22.553 R <sup>2</sup>
Oct. 26.....	2	20	53.229	20	57	31.48			21.749
Oct. 27.....	2	24	45.823	21	01	24.03			21.793
Oct. 29.....	2	32	31.392	21	09	09.57			21.822
Oct. 30.....	2	36	24.352	21	13	02.53			21.822
Nov. 2.....	2	48	02.707	21	24	40.92	5	23	21.787
Nov. 3.....	2	51	55.574	21	28	33.78			21.794
Nov. 4.....	2	55	48.593	21	32	26.85			21.743
Nov. 7.....	3	08	26.758	21	45	04.99			21.768
Nov. 8.....	3	12	19.571	21	48	57.83			21.741
Nov. 10.....	3	20	05.095	21	56	43.27			21.825
Nov. 11.....	3	23	57.989	22	00	36.21			21.779
Nov. 15.....	3	39	29.292	22	16	07.49			21.802
Nov. 19.....	3	55	01.782	22	31	39.96			21.822
Nov. 24.....	4	15	27.438	22	52	05.65			21.788
Nov. 25.....	4	18	21.372	22	54	59.56			21.812
Nov. 30.....	4	38	45.780	23	15	24.09			21.690 R <sup>2</sup>
Mean <sup>3</sup> .....							5	23	21.792

<sup>1</sup> The times of the signals received at Zikawei as published in the report by Lambert (see footnote on p. 1) are given to only two decimal places of seconds. In this computation we have carried the differences between Niu and Zikawei to three decimal places in order to make this table consistent with those following. Although the third decimal place may seem to indicate a fictitious accuracy, it was deemed desirable to carry this decimal place in the computations.

<sup>2</sup> The published times of the Zikawei signals appear to be in error in the minutes in a few instances and they have been arbitrarily changed in this table. Most of these changes have been verified by comparison with the San Diego records of the same signals.

<sup>3</sup> Rejections were made somewhat arbitrarily according to a rule which has been used by the Coast and Geodetic Survey for a number of years in its longitude computations. (See Coast and Geodetic Survey Special Pub. No. 14, fifth edition, p. 80.) Individual values which differed so much from the normal values as to be obviously in error were first rejected. A preliminary mean was then taken and additional rejections were made of values which differed 0.07 or more from this mean. After the final mean was taken some of the rejected values might be found to differ from it less than 0.07, but nevertheless they were allowed to remain as rejected values. It was found that this rule gave about the same rejections as the rule sometimes used by this bureau of rejecting values which differ from the mean by more than  $3\frac{1}{2}$  times the probable error of a single value.

<sup>4</sup> Weight of this mean equals 17.

Comparison of local sidereal times at Niu and Zikawei—Continued

SAIGON SIGNALS NO. 19

Date, 1926	Sidereal time of 300th beat						Difference, Niu minus Zikawei		
	Niu			Zikawei <sup>1</sup>					
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 30.....	3	34	13.344	22	10	51.49	5	23	21.854
Nov. 3.....	3	49	00.329	22	25	38.48			21.849
Nov. 8.....	4	07	20.203	22	44	58.43			21.773
Nov. 9.....	4	12	58.123	22	49	36.28			21.843
Nov. 13.....	4	27	40.657	23	04	18.83			21.827
Nov. 18.....	4	49	41.026	23	26	19.16			21.866
Nov. 23.....	5	09	10.353	23	45	48.55			21.803
Nov. 25.....	5	17	35.798	23	54	13.97			21.828
Mean <sup>4</sup> .....							5	23	21.830

<sup>1</sup> See footnote 1 on p. 14.

<sup>4</sup> Weight of this mean equals 8.

Comparison of local sidereal times at Niu and San Diego

HONOLULU SIGNALS NO. 16

Date, 1926	Sidereal time of 306th beat						Difference, San Diego minus Niu		
	Niu			San Diego					
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Oct. 8.....	1	09	10.943	3	51	17.833	2	42	06.890
Oct. 11.....	1	20	47.898	4	02	54.777			06.879
Oct. 12.....	1	25	39.281	4	07	46.181			06.900
Oct. 14.....	1	33	23.998	4	15	30.896			06.898
Oct. 15.....	1	37	16.340	4	19	23.243			06.903
Oct. 19.....	1	52	46.157	4	34	53.133			06.976
Oct. 20.....	1	56	38.703	4	38	45.637			06.934
Oct. 26.....	2	20	53.229	5	03	00.130			06.901
Oct. 27.....	2	24	45.823	5	06	52.736			06.913
Oct. 29.....	2	32	31.392	5	14	38.311			06.919
Oct. 30.....	2	36	24.352	5	18	31.254			06.902
Nov. 2.....	2	48	02.707	5	30	09.638	2	42	06.931
Nov. 3.....	2	51	55.574	5	34	02.498			06.924
Nov. 4.....	2	55	48.593	5	37	55.537			06.944
Nov. 5.....	2	59	41.706	5	41	48.640			06.934
Nov. 7.....	3	08	26.758	5	50	33.707			06.949
Nov. 8.....	3	12	19.571	5	54	26.599			07.028 R <sup>1</sup>
Nov. 9.....	3	15	13.039	5	57	19.994			06.955
Nov. 10.....	3	20	05.095	6	02	12.001			06.906
Nov. 11.....	3	23	57.989	6	06	04.894			06.905
Nov. 13.....	3	30	44.347	6	12	51.258			06.911
Nov. 15.....	3	39	29.292	6	21	36.167			06.875
Nov. 18.....	3	51	08.675	6	33	15.580			06.905
Nov. 19.....	3	55	01.782	6	37	08.669			06.887
Nov. 23.....	4	10	34.932	6	52	41.861			06.929
Nov. 24.....	4	15	27.438	6	57	34.343			06.905
Nov. 25.....	4	18	21.372	7	00	28.247			06.875
Nov. 27.....	4	26	07.467	7	08	14.360			06.893
Nov. 28.....	4	30	59.781	7	13	06.672			06.891
Nov. 29.....	4	34	52.792	7	16	59.703			06.911
Nov. 30.....	4	38	45.780	7	20	52.678			06.898
Mean <sup>2</sup> .....							2	42	06.911

<sup>1</sup> See footnote 2 on p. 14.

<sup>2</sup> Weight of this mean equals 30.

## Comparison of local sidereal times at Niu and San Diego—Continued

## SAIGON SIGNALS NO. 19

Date, 1926	Sidereal time of 300th beat				Difference, San Diego minus Niu		
	Niu		San Diego				
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	
Oct. 30.....	3	34	13.344	6	16	20.241	2 42 06.897
Nov. 3.....	3	49	00.329	6	31	07.255	06.926
Nov. 8.....	4	07	20.203	6	49	27.234	07.031 R <sup>1</sup>
Nov. 9.....	4	12	58.123	6	55	05.077	06.954
Nov. 13.....	4	27	40.657	7	09	47.617	06.960
Nov. 15.....	4	39	01.630	7	21	08.523	06.893
Nov. 18.....	4	49	41.026	7	31	47.941	06.915
Nov. 23.....	5	09	10.353	7	51	17.300	06.947
Nov. 25.....	5	17	35.798	7	59	42.713	06.915
Mean <sup>3</sup> .....							2 42 06.926

<sup>3</sup> Weight of this mean equals 8.

## HONOLULU SIGNALS NO. 31

Date, 1926	Sidereal time of 306th beat				Difference, San Diego minus Niu		
	Niu		San Diego				
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	
Oct. 11.....	11	23	23.844	14	05	30.742	2 42 06.898
Oct. 12.....	11	27	16.071	14	09	22.929	06.858
Oct. 13.....	11	31	08.452	14	13	15.278	06.826 R <sup>1</sup>
Oct. 14.....	11	35	00.847	14	17	07.761	06.914
Oct. 15.....	11	38	53.174	14	21	00.094	06.920
Oct. 18.....	11	50	30.598	14	32	37.513	06.915
Oct. 19.....	11	54	23.025	14	36	29.963	06.938
Oct. 20.....	11	58	15.645	14	40	22.570	06.925
Oct. 21.....	12	02	08.256	14	44	15.175	06.919
Oct. 22.....	12	06	00.991	14	48	07.907	06.916
Oct. 25.....	12	18	37.612	15	00	44.511	06.899
Oct. 26.....	12	22	30.133	15	04	37.064	06.931
Oct. 27.....	12	26	22.725	15	08	29.661	06.936
Oct. 28.....	12	30	15.511	15	12	22.411	06.900
Oct. 29.....	12	34	08.490	15	16	15.398	06.908
Nov. 1.....	12	45	46.905	15	27	53.820	2 42 06.915
Nov. 2.....	12	49	39.712	15	31	46.657	06.945
Nov. 3.....	12	53	32.655	15	35	39.634	06.979
Nov. 4.....	12	57	25.664	15	39	32.648	06.984 R <sup>1</sup>
Nov. 6.....	13	06	10.970	15	48	17.868	06.898
Nov. 7.....	13	10	03.881	15	52	10.809	06.928
Nov. 8.....	13	13	56.513	15	56	03.479	06.966
Nov. 9.....	13	17	49.301	15	59	56.202	06.901
Nov. 10.....	13	21	42.244	16	03	49.049	06.805 R <sup>1</sup>
Nov. 11.....	13	25	34.989	16	07	41.860	06.871
Nov. 12.....	13	29	27.755	16	11	34.699	06.944
Nov. 13.....	13	33	20.546	16	15	27.364	06.818 R <sup>1</sup>
Nov. 14.....	13	37	13.255	16	19	20.229	06.974
Nov. 15.....	13	41	06.496	16	23	13.291	06.795 R <sup>1</sup>
Nov. 17.....	13	48	52.684	16	30	59.613	06.929
Nov. 24.....	14	17	04.599	16	59	11.496	06.897
Nov. 25.....	14	20	57.629	17	03	04.537	06.908
Nov. 26.....	14	24	50.621	17	06	57.542	06.921
Nov. 27.....	14	28	43.655	17	10	50.750	07.095 R <sup>1</sup>
Nov. 28.....	14	32	36.858	17	14	43.758	06.900
Nov. 29.....	14	36	29.840	17	18	36.743	06.903
Nov. 30.....	14	40	22.827	17	22	29.801	06.974
Mean <sup>4</sup> .....							2 42 06.920

<sup>1</sup> See footnote 2 on p. 14.<sup>4</sup> Weight of this mean equals 31.

Computation of transmission times

[See p. 10]

Longitude station	Radio transmitting station	Distance	Difference in distance	Correction for transmission time
Niu.....	Honolulu.....	km. 12	km.	s.
Zikawei.....	do.....	7,950	-7,938	+0.026
Niu.....	Saigon.....	10,140		
Zikawei.....	do.....	2,110	+8,030	-0.027
San Diego.....	Honolulu.....	4,222		
Niu.....	do.....	12	+4,210	-0.014
San Diego.....	Saigon.....	13,319		
Niu.....	do.....	10,140	+3,179	-0.011

Differences of longitude

NIU TO ZIKAWEI

Radio signal	Computed difference of longitude	Weight	Correction for transmission time	Corrected difference of longitude
	<i>h. m. s.</i>		<i>s.</i>	<i>h. m. s.</i>
Honolulu, No. 16.....	5 23 21.792	17	+0.026	5 23 21.818
Saigon, No. 19.....	21.830	8	-0.027	21.803
Weighted mean.....				5 23 21.813
Probable error.....				±.005

SAN DIEGO TO NIU

	<i>h. m. s.</i>	Weight	<i>s.</i>	<i>h. m. s.</i>
Honolulu, No. 16.....	2 42 06.911	30	-0.014	2 42 06.897
Saigon, No. 19.....	06.926	8	-0.011	06.915
Honolulu, No. 31.....	06.920	31	-0.014	06.906
Weighted mean.....				2 42 06.903
Probable error.....				±.003

Least-squares adjustment

[Fixed difference of longitude San Diego to Zikawei (main polygon) = 8<sup>h</sup> 05<sup>m</sup> 28<sup>s</sup>.733]

Stations	Observed difference of longitude	Correction symbol	Weight	Least-squares correction	Adjusted difference of longitude
	<i>h. m. s.</i>			<i>s.</i>	<i>h. m. s.</i>
San Diego-Niu.....	2 42 06.903	$v_1$	69	+0.005	2 42 06.908
Niu-Zikawei.....	5 23 21.813	$v_2$	25	+0.012	5 23 21.825
San Diego-Zikawei.....	8 05 28.716				8 05 28.733

Fixed difference, San Diego to Zikawei, minus observed difference equals  $+0.017$ .

Therefore,

$$v_1 + v_2 - 0.017 = 0$$

or

$$v_1 = 0.017 - v_2$$

Taking the weights into consideration, the quantity to be made a minimum is

$$69v_1^2 + 25v_2^2$$

Substituting the value of  $v_1$  above, this reduces to

$$69(0.017 - v_2)^2 + 25v_2^2$$

Differentiating and equating to zero we obtain

$$138v_2 - 2.346 + 50v_2 = 0$$

$$v_2 = +0.012$$

$$v_1 = +0.005$$

#### FINAL LONGITUDE

A recent publication of the International Longitude Commission<sup>6</sup> gives the longitudes of 40 stations which were determined in the world longitude operations of 1926. As given there the longitude of San Diego is  $7^{\text{h}} 48^{\text{m}} 48.374$  west of Greenwich, and of Zikawei is  $8^{\text{h}} 05^{\text{m}} 42.893$  east. Applying the adjusted differences given above, we obtain the following result for Niu: **Longitude of Niu =  $10^{\text{h}} 30^{\text{m}} 55.282$  west of Greenwich.**

The published value of Niu given in the report just mentioned is  $10^{\text{h}} 30^{\text{m}} 55.279$  west. The difference,  $0.003$ , between the two values is probably due to somewhat different methods for making rejections in the computations. (See footnote 2, p. 14.)

#### ASTRONOMICAL CONNECTION OF NIU AND OLD CABLE STATION AT HONOLULU

Soon after the completion of the world longitude observations at Niu, an astronomical connection by the wire-telegraph method was made between this station and the old cable longitude station at Honolulu which was determined in 1903. Lieutenant Brown made the observations at Niu and Lieutenant Bainbridge at Honolulu. A straight-telescope transit was obtained from the Washington office for use at the former station.

Longitude differences were determined on four different nights. Unfortunately, the results are quite discordant as can be seen by the following table. As the general instructions of this bureau for longitude work do not require a field computation before leaving a station, provided four or more independent determinations are made, the lack of agreement between the different values was not discovered in time to permit additional determinations except at very great inconvenience and expense.

<sup>6</sup> La Revision des Longitudes Mondiales, Commission internationale des Longitudes, par. T. S. F., Paris, 1929.

The range of values for this difference of longitude is probably greater than for any other difference determined by this bureau since the telegraphic method came into use. The trouble may have been caused by lateral refraction at the Honolulu station or by a defect of the straight-telescope instrument, which had not been used for a

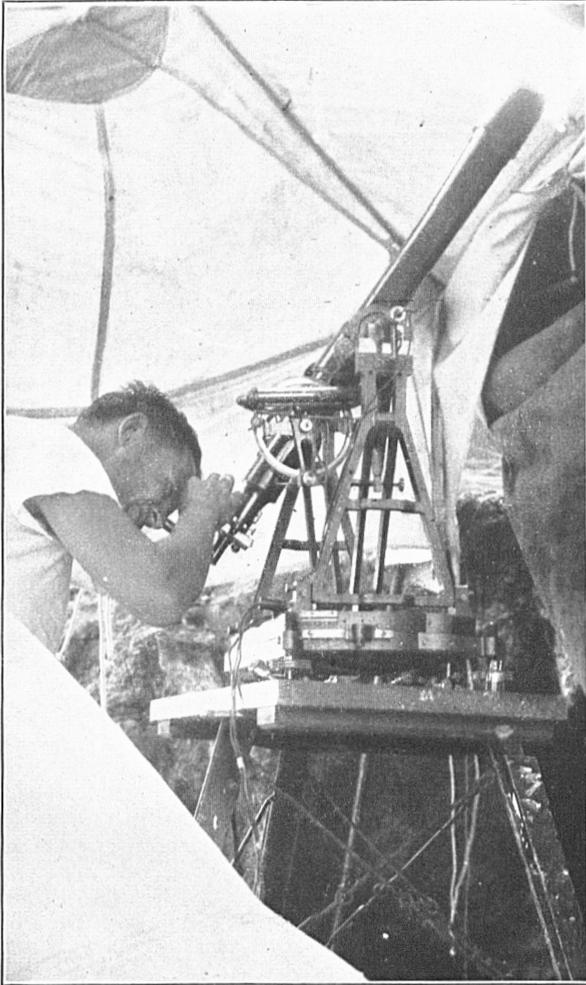


FIGURE 8.—MERIDIAN TELESCOPE

This is an old type of portable astronomical transit. It was used for the radio determination of the old cable longitude station at Honolulu.

number of years. Whatever may have been the reason for the large discrepancies, there is no way of telling definitely what values are most nearly correct, and it was decided to reject all of them, although the first two are in fairly close agreement. A new series of determinations between these two stations will be made some time in the future if it can be done without too great expense.

*Difference of longitude, Niu to Honolulu*

Date	Longitude difference	Date	Longitude difference
Jan. 31..... 1927	s. 32. 400	Feb. 3..... 1927	s. 32. 522
Feb. 1.....	32. 337	Feb. 4.....	32. 624

Reduction of new pier to old pier = +0:015

The cable determination in 1903 gave the longitude of Honolulu as  $10^{\text{h}} 31^{\text{m}} 27^{\text{s}}.732$  west.<sup>7</sup> This value is based on  $5^{\text{h}} 08^{\text{m}} 15^{\text{s}}.784$  west as the adjusted longitude of Washington. However, the 1926 radio determinations, in which Niu is included, gives the longitude of Washington as  $5^{\text{h}} 08^{\text{m}} 15^{\text{s}}.751$  west.<sup>8</sup> If we apply a correction for this change in the Washington longitude, we obtain for the old Honolulu determination a value of  $10^{\text{h}} 31^{\text{m}} 27^{\text{s}}.699$  west.

The longitude obtained for Niu (see p. 18) is  $10^{\text{h}} 30^{\text{m}} 55^{\text{s}}.282$  west, and therefore the difference between the two stations, as derived in this manner, is  $32^{\text{s}}.417$ . This agrees closely with the first one only of the four determinations given above, which, after correction for the distance between the old and new piers, is  $32^{\text{s}}.415$ .

#### DESCRIPTION OF OLD CABLE LONGITUDE STATION AT HONOLULU

The original description of 1903 of the Honolulu cable longitude station reads as follows:<sup>9</sup>

In the grounds of the United States naval station, 88.97 meters north and 505.97 meters east of Harbor Light. The station is marked by a concrete pier 14 by 26 inches in cross section, and 3 feet high, resting on a concrete foundation, 3 by 4 feet in cross section, which in turn rests upon coral rock  $2\frac{1}{2}$  feet below the surface of the ground. North of the center of the pier, and 3.435 meters therefrom, is a galvanized-iron pipe  $2\frac{1}{2}$  feet long set in cement, with its center marked by a copper bolt. This is a point of the Territorial survey.

When the station was visited in 1926, it was found that the marks had been destroyed by building operations of the United States Navy. The approximate position of the old pier was reestablished by means of data furnished by the surveyor general of Hawaii. The station as relocated in 1926 is on the east side of the main building in the naval station grounds. It is  $2\frac{1}{2}$  feet south of the cement walk leading to the north porch steps and 1 foot east of the board walk which is close to the building and parallel to it. The point was remarked with an iron pin driven 2 inches below the surface of the ground.

#### RADIO DETERMINATION IN 1928 OF OLD CABLE LONGITUDE STATION AT HONOLULU

Because of the discordant results obtained in 1927 in connecting Niu with the old cable station at Honolulu, it was decided in the spring of 1928 to make a radio determination of the Honolulu station. This could be done at small expense, since Lieutenant Brown was already at Honolulu making preparations for astronomical work on the outlying reefs and small islands which extend northwest from the main islands of the Hawaiian group. A meridian telescope, a short-wave

<sup>7</sup> See Coast and Geodetic Survey Special Publication No. 110, p. 40.

<sup>8</sup> See publication mentioned in footnote on p. 18.

<sup>9</sup> See Coast and Geodetic Survey Special Publication No. 110, p. 278.

radio receiver, and the necessary auxiliary apparatus were on hand for the work. A telegraphic determination between Niu and Honolulu to check the 1927 determination could not be made because only one set of instruments was available.

Observations were made on April 19 and 20, 1928, and the results for the two nights agreed within 0<sup>o</sup>25'. The mean of the two determinations gave a difference of longitude from Washington of 5<sup>h</sup> 23<sup>m</sup> 11<sup>s</sup>.884. Using the 1926 value of the Washington longitude, this makes the longitude of the Honolulu station 10<sup>h</sup> 31<sup>m</sup> 27<sup>s</sup>.635 west, and the difference between Niu and Honolulu comes out as 32<sup>o</sup>353'. As stated on page 20, the old cable value for Honolulu, reduced to the 1926 value of the Washington longitude, is 10<sup>h</sup> 31<sup>m</sup> 27<sup>s</sup>.699 west.

**RESULTS AT STATION FORT WM. MCKINLEY (near Manila)**

**DESCRIPTION OF STATION**

Longitude station Fort Wm. McKinley is about 6 miles southeast of Manila, P. I., in the grounds of the fort of the same name, on the east end of a spur, about 170 meters north of the officers' club in the eastern part of the reservation. The station is marked by a standard brass-disk triangulation station mark which has the word "TRIANGULATION" in the inscribed legend changed to the words "WORLD LONGITUDE." The disk is set in the top of a concrete monument which tapers from 31 by 36 inches at the surface of the ground to 16 by 24 inches at the top. The monument is 46 inches high and extends 30 inches below the ground to "dobe" rock.

*Local sidereal times of reception of radio signals*

SIGNALS FROM HONOLULU, No. 17 (10.40-10.45; 37 METERS) <sup>1</sup>

Date, 1926	Local sidereal time				Date, 1926	Local sidereal time					
	Beat No. 1		Beat No. 306			Beat No. 1		Beat No. 306			
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>		
Nov. 22.....	22	47	39.703	22	52	40.512	Nov. 28.....	23	10	58.657	
Nov. 23.....		50	33.859		55	34.668	Nov. 29.....		14	51.674	
Nov. 24.....		55	26.354		23	00	27.163	Nov. 30.....		18	44.682

SIGNALS FROM SAIGON, NO. 19 (11.30-11.35; 15,800 METERS)

Date, 1926	Local sidereal time				Date, 1926	Local sidereal time				
	Beat No. 1		Beat No. 300			Beat No. 1		Beat No. 300		
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	
Nov. 8.....	22	37	33.545	22	42	28.147	Nov. 18.....	23	19	54.340
Nov. 9.....		43	11.585		48	06.100	Nov. 19.....		24	22.048
Nov. 10.....		46	27.153		51	21.764	Nov. 22.....		36	17.757
Nov. 11.....		48	38.720		53	33.331	Nov. 23.....		39	23.658
Nov. 14.....	23	00	29.601	23	05	24.137	Nov. 24.....		44	03.269
Nov. 15.....		09	14.938		14	09.492				

SIGNALS FROM SAIGON, NO. 23 (19.00-19.05; 15,800 METERS)

Nov. 8.....	6	08	02.236	6	12	56.841	Nov. 19.....	6	55	13.956	7	00	08.537	
Nov. 10.....		17	26.167		22	20.772	Nov. 24.....		7	14	20.072		19	14.656
Nov. 14.....		31	08.179		36	02.775								

<sup>1</sup> These short-wave signals were not used in computing the longitude of Fort Wm. McKinley. See p. 9.

COMPUTATION OF LONGITUDE, STATION FORT WM. MCKINLEY

The computation of longitude at Fort Wm. McKinley was made in the same way as at station Niu (see p. 13) with the one exception, which has already been noted on pages 2 and 3. Because of the small number of observations at station Fort Wm. McKinley, differences with Niu, as well as with the two fundamental stations, Zikawei and San Diego, were used in deriving the final value of the longitude.

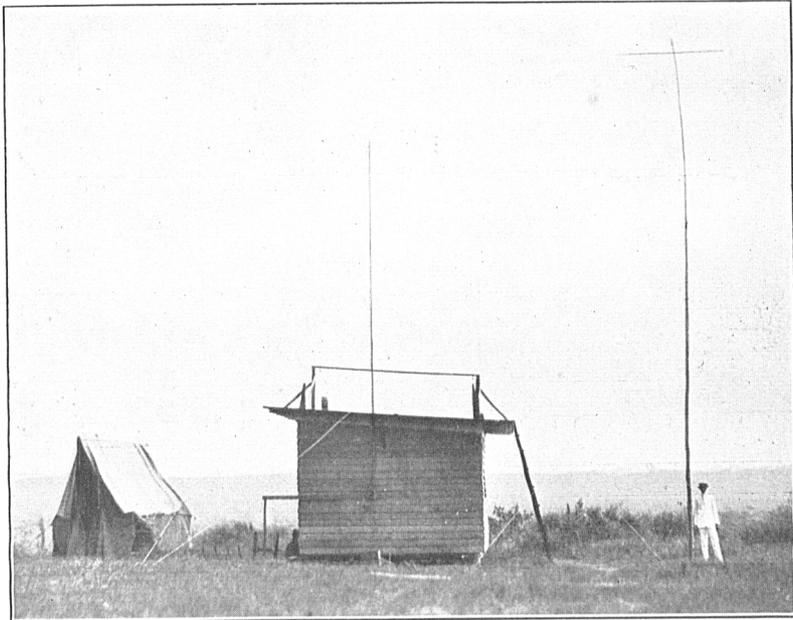


FIGURE 9.—OBSERVATORY AT FORT WILLIAM MCKINLEY (NEAR MANILA)  
This is on the military reservation about 6 miles southeast of Manila.

*Comparison of local sidereal times at Niu and Fort Wm. McKinley*

SAIGON SIGNALS NO. 19

Date, 1926	Sidereal time of 300th beat						Difference, Niu minus Fort Wm. McKinley		
	Niu			Fort Wm. McKinley					
	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>	<i>h.</i>	<i>m.</i>	<i>s.</i>
Nov. 8.....	4	07	20.203	22	42	28.147	5	24	52.056
Nov. 9.....		12	58.123		48	06.100			52.023
Nov. 15.....		39	01.630	23	14	09.492			52.138
Nov. 18.....		49	41.026		24	48.945			52.031
Nov. 23.....	5	09	10.353	44	18.	212			52.141
Mean <sup>1</sup> .....							5	24	52.088

SAIGON SIGNALS NO 23

Nov. 19.....	12	25	00.709	7	00	08.537	5	24	52.172
Mean <sup>2</sup> .....							5	24	52.172

<sup>1</sup> Weight of this mean equals 5.

<sup>2</sup> Weight of this mean equals 1.

Comparison of local sidereal times at Fort Wm. McKinley and San Diego

SAIGON SIGNALS NO. 19

Date, 1926	Sidereal time of 300th beat		Difference, San Diego minus Fort Wm. Mc- Kinley
	Fort Wm. Mc- Kinley	San Diego	
	<i>h. m. s.</i>	<i>h. m. s.</i>	<i>h. m. s.</i>
Nov. 8.....	22 42 28.147	6 49 27.234	8 06 59.087
Nov. 9.....	48 06.100	55 05.077	58.977
Nov. 10.....	51 21.764	58 20.812	59.048
Nov. 11.....	53 33.331	7 00 32.293	58.962
Nov. 14.....	23 05 24.137	12 23.186	59.049
Nov. 15.....	14 09.492	21 08.523	59.031
Nov. 18.....	24 48.945	31 47.941	58.996
Nov. 19.....	29 16.638	36 15.691	59.053
Nov. 22.....	41 12.362	48 11.357	58.995
Nov. 23.....	44 18.212	51 17.300	59.088
Nov. 24.....	48 57.877	55 56.888	59.011
Mean <sup>1</sup> .....			8 06 59.027

<sup>1</sup> Weight of this mean equals 11.

Comparison of local sidereal times at Fort Wm. McKinley and Zikawei

SAIGON SIGNALS NO. 19

Date, 1926	Sidereal time of 300th beat		Difference, Zikawei minus Fort Wm. McKinley
	Fort Wm. Mc- Kinley	Zikawei <sup>1</sup>	
	<i>h. m. s.</i>	<i>h. m. s.</i>	<i>h. m. s.</i>
Nov. 8.....	22 42 28.147	22 43 58.43	0 01 30.283
Nov. 9.....	48 06.100	49 36.28	30.180 R <sup>2</sup>
Nov. 10.....	51 21.764	52 52.02	30.256
Nov. 11.....	53 33.331	55 03.52	30.189
Nov. 11.....	23 05 24.137	23 06 54.42	30.283
Nov. 18.....	24 48.945	26 19.16	30.215
Nov. 19.....	29 16.638	30 46.91	30.272
Nov. 22.....	41 12.362	42 42.64	30.278
Nov. 23.....	44 18.212	45 48.55	30.338 R <sup>2</sup>
Nov. 24.....	48 57.877	50 28.11	30.233
Mean <sup>3</sup> .....			0 01 30.251

<sup>1</sup> See footnote 1 on p. 14.

<sup>2</sup> See footnote 2 on p. 14.

<sup>3</sup> Weight of this mean equals 8.

Computation of transmission times

[See p. 10]

Longitude station	Radio transmitting station	Distance	Difference in distance	Correc- tion for trans- mission time
		<i>km.</i>	<i>km.</i>	<i>s.</i>
Niu.....	Saigon.....	10,140		
Fort Wm. McKinley.....	..do.....	1,700	+8,440	-0.028
San Diego.....	..do.....	13,319		
Fort Wm. McKinley.....	..do.....	1,700	+11,619	-0.039
Zikawei.....	..do.....	2,110		
Fort Wm. McKinley.....	..do.....	1,700	+410	-0.001

*Differences of longitude*

NIU TO FORT WM. MCKINLEY

Radio signal	Computed difference of longitude		Weight	Correc- tion for trans- mission time	Corrected difference of longitude	
	<i>h. m.</i>	<i>s.</i>			<i>h. m.</i>	<i>s.</i>
Saigon, No. 19.....	5	24 52.088	5	<i>s.</i> -0.028	5	24 52.060
Saigon, No. 23.....		52.172	1	-0.028		52.144
Weighted mean.....					5	24 52.074
Probable error.....						±0.021

SAN DIEGO TO FORT WM. MCKINLEY

Saigon, No. 19.....	8	06 59.027	11	-0.039	8	06 58.988
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ZIKAWEI TO FORT WM. MCKINLEY

Saigon, No. 19.....	0	01 30.251	8	-0.001	0	01 30.250
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*Least-squares adjustment*

[Fixed differences of longitude are: San Diego to Zikawei (main polygon), 8<sup>h</sup> 05<sup>m</sup> 28<sup>s</sup>.733 and Niu to Zikawei (see p. 17), 5<sup>h</sup> 23<sup>m</sup> 21<sup>s</sup>.825]

Stations	Observed difference of longitude		Correc- tion symbol	Weight	Least- squares correction	Adjusted difference of longitude	
	<i>h. m.</i>	<i>s.</i>				<i>h. m.</i>	<i>s.</i>
San Diego-Fort Wm. McKinley.....	8	06 58.988	$v_3$	11	<i>s.</i> -0.003	8	06 58.985
Zikawei-Fort Wm. McKinley.....	0	01 30.250	$v_1$	8	+0.002	0	01 30.252
San Diego-Zikawei.....	8	05 28.738				8	05 28.733
Niu-Fort Wm. McKinley.....	5	24 52.074	$v_2$	6	+0.003	5	24 52.077
Zikawei-Fort Wm. McKinley.....	0	01 30.250	$v_1$	8	+0.002	0	01 30.252
Niu-Zikawei.....	5	23 21.824				5	23 21.825

Fixed difference, San Diego to Zikawei, minus observed difference equals  $-0^{\circ}005$ , and fixed difference, Niu to Zikawei, minus observed difference equals  $+0^{\circ}001$ .

Therefore,

$$v_3 - v_1 + 0.005 = 0$$

and

$$v_2 - v_1 - 0.001 = 0$$

or

$$v_3 = v_1 - 0.005$$

and

$$v_2 = v_1 + 0.001.$$

Taking the weights into consideration the quantity to be made a minimum is

$$8 v_1^2 + 6 v_2^2 + 11 v_3^2.$$

Substituting the values of  $v_2$  and  $v_3$  above, this reduces to

$$8 v_1^2 + 6 (v_1 + 0.001)^2 + 11 (v_1 - 0.005)^2.$$

Differentiating and equating to zero we obtain

$$16 v_1 + 12 v_1 + 0.012 + 22 v_1 - 0.110 = 0,$$

$$v_1 = +0.002,$$

$$v_2 = +.003,$$

$$v_3 = -.003.$$



FIGURE 10.—INSTRUMENTAL EQUIPMENT AT FORT WILLIAM MCKINLEY

The transit is shown on the concrete pier near the center of the picture and the chronograph on the bench at the extreme right. The rest of the instruments are mostly radio equipment.

## FINAL LONGITUDE

The longitude of Zikawei, as given in the publication referred to in the footnote on page 18, is  $8^{\text{h}} 05^{\text{m}} 42^{\text{s}}.893$  east of Greenwich, and the longitude of San Diego, as given in the same publication, is  $7^{\text{h}} 48^{\text{m}} 48^{\text{s}}.374$  west. Applying the adjusted differences given above, we obtain the following result for Fort Wm. McKinley: **Longitude of Fort Wm. McKinley =  $8^{\text{h}} 04^{\text{m}} 12^{\text{s}}.641$  east of Greenwich.**

The published value of Fort Wm. McKinley given in the publication referred to above is  $8^{\text{h}} 04^{\text{m}} 12^{\text{s}}.656$  east. As stated in connection with a corresponding discrepancy at station Niu (see p. 18), the difference of  $0^{\circ}.015$  is probably due to somewhat different methods for making rejections in the computations.

**ASTRONOMICAL CONNECTION OF FORT WM. MCKINLEY AND OLD CABLE STATION AT MANILA**

During the spring of 1927 Lieutenant Sipe and Lieut. J. A. McCormick made an astronomical connection between the station at Fort Wm. McKinley and the old cable longitude station at Manila, which was determined in 1903. Lieutenant McCormick occupied the Manila station, using one of the old-type straight-telescope transits.

Longitude differences were determined on four different nights but the result for the last night had to be rejected. The following table contains the results for the other three nights:

*Difference of longitude, Fort Wm. McKinley to Manila*

Date, 1927	Longitude difference
Mar. 30.....	s. 20.317
Mar. 31.....	20.308
Apr. 1.....	20.302
Mean.....	20.309
Probable error.....	$\pm .003$

The cable determination of 1903 gave the longitude of Manila as  $8^{\text{h}} 03^{\text{m}} 52^{\text{s}}.202$  east.<sup>10</sup>

This value is based on  $5^{\text{h}} 08^{\text{m}} 15^{\text{s}}.784$  west as the adjusted longitude of Washington. As stated on page 20, the 1926 radio determination of Washington is  $5^{\text{h}} 08^{\text{m}} 15^{\text{s}}.751$  west. Applying a correction to the old Manila longitude to take account of this change we obtain  $8^{\text{h}} 03^{\text{m}} 52^{\text{s}}.235$  east as the old cable value for Manila based on the new datum.

The adjusted longitude of Fort Wm. McKinley (see above) is  $8^{\text{h}} 04^{\text{m}} 12^{\text{s}}.641$  east. If we subtract from this the difference of longitude given above between that station and the Manila station, we obtain for the latter a value of  $8^{\text{h}} 03^{\text{m}} 52^{\text{s}}.332$  east. This gives a discrepancy of  $0^{\circ}.097$  between the old and new determinations. We can safely attribute a rather large percentage of this discrepancy to the cable determination because of errors inherent in that method. The

<sup>10</sup> See Coast and Geodetic Survey Special Publication No. 110, p. 40.

agreement between the two values is therefore about as close as could be expected.

#### DESCRIPTION OF OLD CABLE LONGITUDE STATION AT MANILA

The original description of the cable longitude station at Manila reads as follows:<sup>11</sup>

In the walled city of Manila, in the block fronting on Calle Audiencia, between Calle Postigo and Calle Claveria, and 9.48 meters from the house line on the first-named street. Station is in a quadrangle formed by the foundation of a projected government building (Spanish), and opposite the plaza in front of the government building commonly known as the Ayuntamiento. Two massive granite blocks were set for the instrument piers, their centers being in an east and west line and 5.5 feet apart. The eastern pier is the longitude station. Cathedral dome, a triangulation station, is 46.98 meters south and 100.67 meters east of the station.

When the station was recovered in 1927, there was only one granite pier standing. This was found to be the old longitude pier. Check measurements were made to the cathedral dome. The 1927 description states that the station is on the east side of a proposed palace building on Calle Gral. Luna, about 50 meters back from Calle Aduana and 10.65 meters from the sidewalk curb of Calle Gral. Luna. The station is marked by a granite block 4 feet high and 18 by 24 inches in cross section.

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<sup>11</sup> See Coast and Geodetic Survey Special Publication No. 110, p. 278.



## PUBLICATION NOTICES

The Coast and Geodetic Survey maintains a mailing list of persons interested in its airway maps, nautical charts, and miscellaneous publications. On the issuance of new or revised editions descriptive circulars are promptly mailed to those interested in the subject matter.

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