



# Multi-GNSS Positioning with the New M-PAGES Software

Bryan Stressler  
Geosciences Research Division  
[bryan.stressler@noaa.gov](mailto:bryan.stressler@noaa.gov)  
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# Outline

- Background on the evolution of GNSS, motivating the development of M-PAGES
- Discuss the products and services at NGS that will use M-PAGES
- Overview of the M-PAGES processing strategy, and how it compares to the legacy PAGES software
- Demonstrate M-PAGES performance for a range of use cases
- Preview the expected timeline for M-PAGES integration into NGS products and services

# Key Points

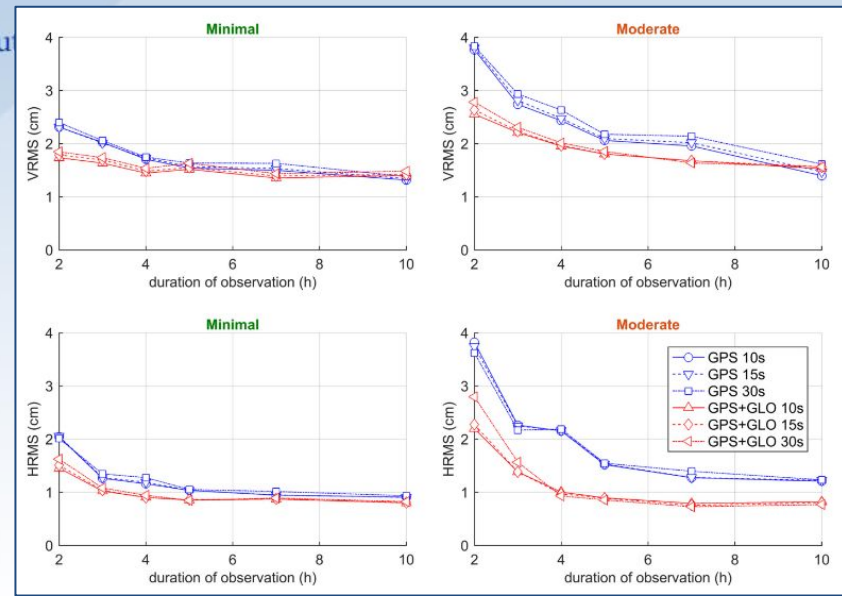
- M-PAGES is capable of processing GNSS data for all dual-frequency systems
- Improved positioning with multi-GNSS data can be demonstrated with M-PAGES
- M-PAGES is still under active development, but OPUS-S integration is underway

# Why replace PAGES?

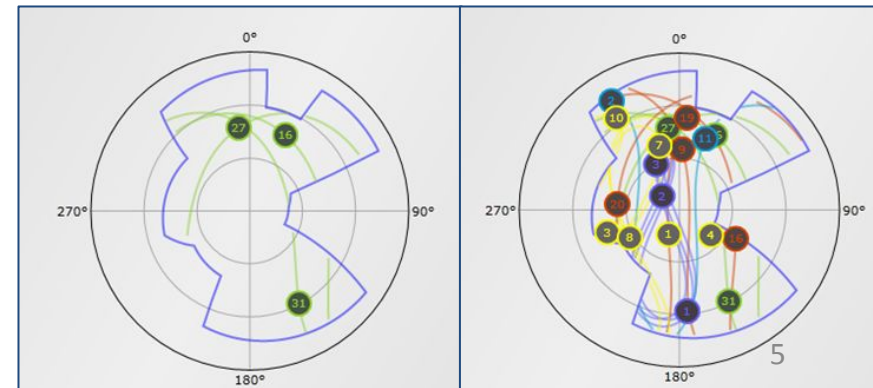
- PAGES = Program for the Adjustment of GPS Ephemerides
- Double-difference baseline processing (GPS L1/L2 only)
- Currently used in production at NGS for:
  - Online Positioning User Service (OPUS)
  - NOAA CORS Network (NCN) monitoring
  - Precise orbit determination
- *Unable to make use of new GNSS constellations or new frequencies*

# Why replace PAGES?

- More satellites = better positioning!
  - Improved geometry
  - Better coverage when signals are obstructed (bottom right)
- Various studies have already demonstrated the improvements in positioning with added systems (top right)

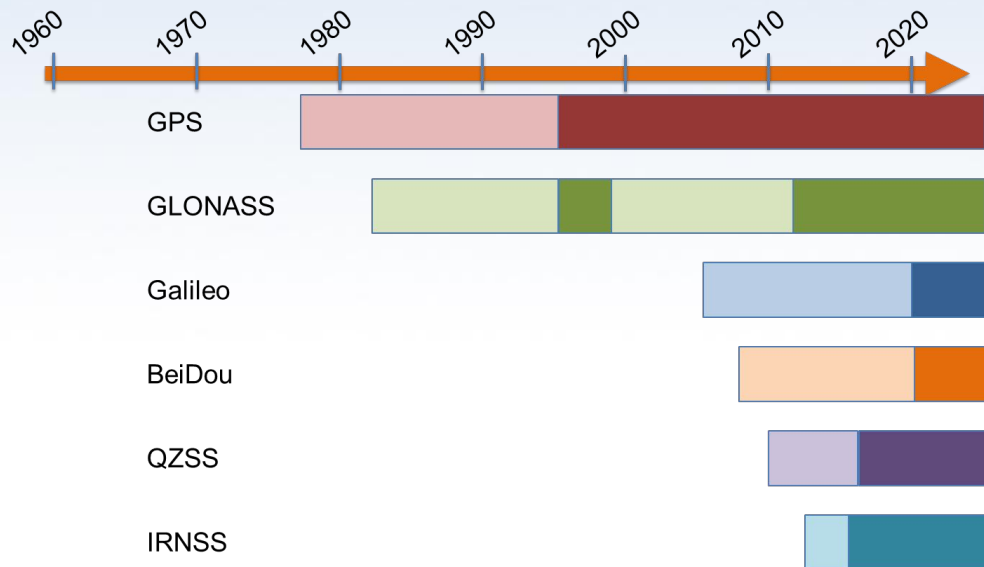


From Jamieson & Gillins 2018 (Above)



# Background

- GNSS = Global Navigation Satellite System
- GNSS constellations:
  - GPS (US)
  - GLONASS (Russia)
  - Galileo (EU)
  - BeiDou (China)
  - QZSS (Japan; regional)
  - IRNSS (India; regional)
- Currently there are >100 GNSS satellites in orbit!



From Heck 2017. For additional background on multi-GNSS see:  
[https://www.ngs.noaa.gov/web/science\\_edu/webinar\\_series/positioning-multi-gnss-world.shtml](https://www.ngs.noaa.gov/web/science_edu/webinar_series/positioning-multi-gnss-world.shtml)

# GPS

- Constellation consists of satellites in medium earth orbit (MEO)
  - ~20,000 km orbit altitude
  - 2 revolutions per day
- Code division multiple access (CDMA) system
- GPS satellites historically transmitted signals on two frequencies
  - L1: 1575.42 MHz
  - L2: 1227.60 MHz
- Ongoing GPS modernization since the 2000s
  - New civil signals L1C, L2C
  - New L5 frequency: 1176.45 MHz



[https://www.faa.gov/about/office\\_org/headquarters\\_offices/ato/service\\_units/techops/navservices/gnss/gps](https://www.faa.gov/about/office_org/headquarters_offices/ato/service_units/techops/navservices/gnss/gps)



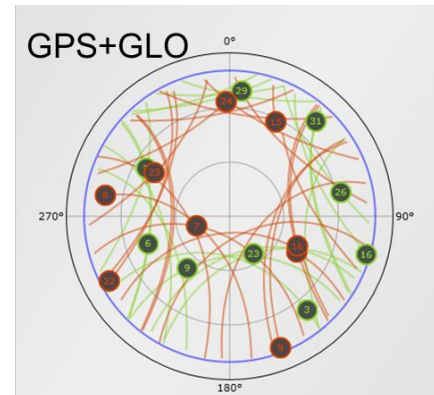
# GLONASS

- Originally launched in 1980s
- MEO orbits with higher inclination angle = better coverage at polar latitudes
- Legacy satellites use frequency division multiple access (FDMA) based around G1 and G2 frequencies:
  - FDMA poses challenges for ambiguity resolution
- GLONASS modernization ongoing
  - Third frequency (G03): 1202.025 MHz
  - Future CDMA satellites planned

Table 11 : RINEX Version 4.00 GLONASS Observation Codes

GNSS System	Freq. Band / Frequency	Channel or Code	Observation Codes			
			Pseudo Range	Carrier Phase	Doppler	Signal Strength
GLONASS	G1/ 1602+k*9/16 k= -7....+12	C/A	C1C	L1C	D1C	S1C
		P	C1P	L1P	D1P	S1P
	G1a/ 1600.995	L1OCd	C4A	L4A	D4A	S4A
		L1OCp	C4B	L4B	D4B	S4B
		L1OCd+ L1OCp	C4X	L4X	D4X	S4X
	G2/ 1246+k*7/16	C/A	C2C	L2C	D2C	S2C
		P	C2P	L2P	D2P	S2P
	G2a/ 1248.06	L2CSI	C6A	L6A	D6A	S6A
		L2OCp	C6B	L6B	D6B	S6B
		L2CSI+ L2OCp	C6X	L6X	D6X	S6X
	G3 / 1202.025	I	C3I	L3I	D3I	S3I
		Q	C3Q	L3Q	D3Q	S3Q
		I+Q	C3X	L3X	D3X	S3X

<https://igs.org/news/rinex-4-now-available/>



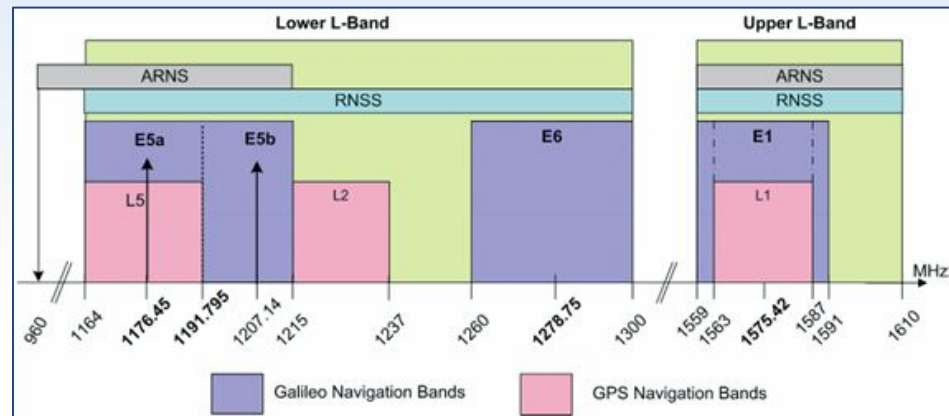
Sky plot for GNSS station at polar latitude

<http://www.gnssplanningonline.com>



# Galileo

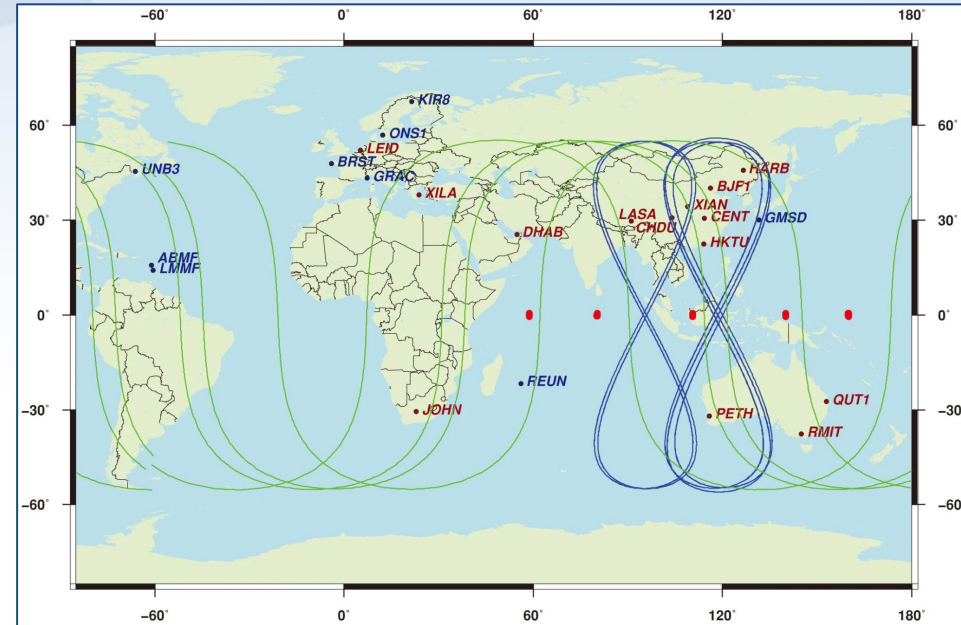
- Galileo system launched by the EU
- MEO orbits
- Global system with three frequencies:
  - E1, E5, E6
  - E5 consists of E5a and E5b frequencies
  - E1/E5a align with GPS L1/L5
- CDMA system



<https://galileognss.eu/galileo-frequency-bands/>

# BeiDou

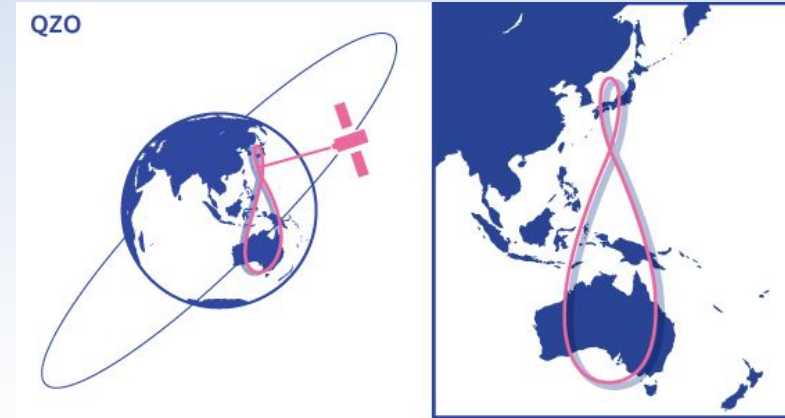
- Constellation consists of satellites in three types of orbit:
  - MEO
  - Inclined geosynchronous orbit
  - Geostationary orbit
- Multiple satellite generations already launched
  - BDS I-III
- Transmits signals on three frequencies
- CDMA system



Lou et al., 2014

# QZSS

- QZSS = Quasi Zenith Satellite System
- Regional system
- Frequencies: L1/L2/L5/L6
  - Designed for consistency with GPS



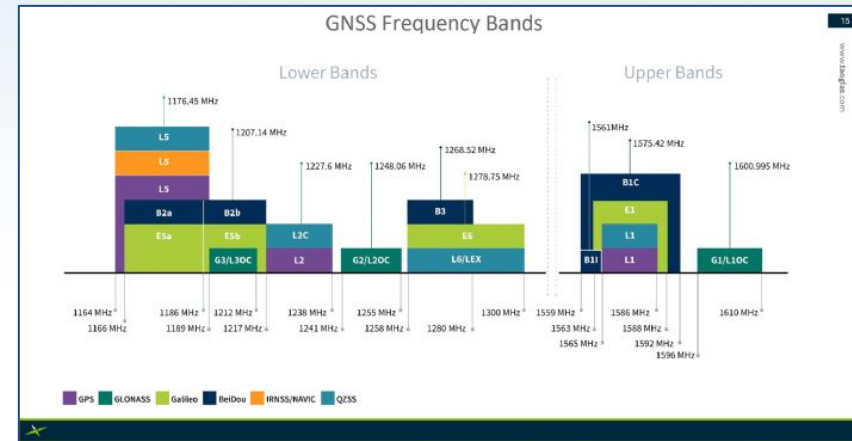
<https://qzss.go.jp/en/technical/technology/orbit.html>



[https://qzss.go.jp/en/overview/services/sv01\\_what.html](https://qzss.go.jp/en/overview/services/sv01_what.html)

# Challenges of Multi-GNSS Positioning

- Different time systems
- Frequency-dependent errors
- Availability of antenna calibrations
- Availability of reference stations tracking all GNSS
- GLONASS ambiguity resolution (FDMA)



<https://www.everythingrf.com/community/navigating-the-l1-l2-and-l5-band-options-for-gnss>

# Why replace PAGES?

- Written in Fortran; Difficult to extend/maintain with current staff
- Does not support RINEX versions  $> 2$ 
  - RINEX version  $\geq 3$  required for all GNSS and all new signal types
- Unable to make use of new GNSS constellations or new frequencies

# M-PAGES Software

- M-PAGES = Multi-GNSS PAGES
- Single difference baseline processing using pseudorange and carrier phase measurements
- Capable of processing data from all GNSS constellations with two or more frequencies
- Written primarily in C++ with supporting scripts in Python

The screenshot shows the M-PAGES website interface. At the top, the title "M-PAGES" is displayed. Below it is a navigation menu with tabs for "Main Page", "Related Pages", "Namespaces", "Classes", and "Files". The "Main Page" tab is selected. On the left side, there is a sidebar menu with a tree view containing the following items: "M-PAGES", "File Formats", "Main Programs", "Data Processing", "sinex2siteInfo", "convert\_sif", "Todo List", "Namespaces", "Classes", and "Files". The main content area on the right is titled "M-PAGES Documentation" and contains the following text: "M-PAGES or Multi-GNSS PAGES is NGS's effort to meet the obligations to the International GNSS Service (IGS) for the production of precise GPS orbits and clock corrections. M-PAGES is capable of processing data from all GNSS constellations with two or more frequencies. M-PAGES will be integrated into the Online Positioning and User Services (OPUS) CORS monitoring and GPS orbit production, to provide precise GPS orbits and clock corrections. Questions can be addressed to the M-PAGES project manager. The project plan and quarterly status reports are available. Issues are tracked using the NGS JIRA system. The source code is kept under version control. This documentation was created with Doxygen.

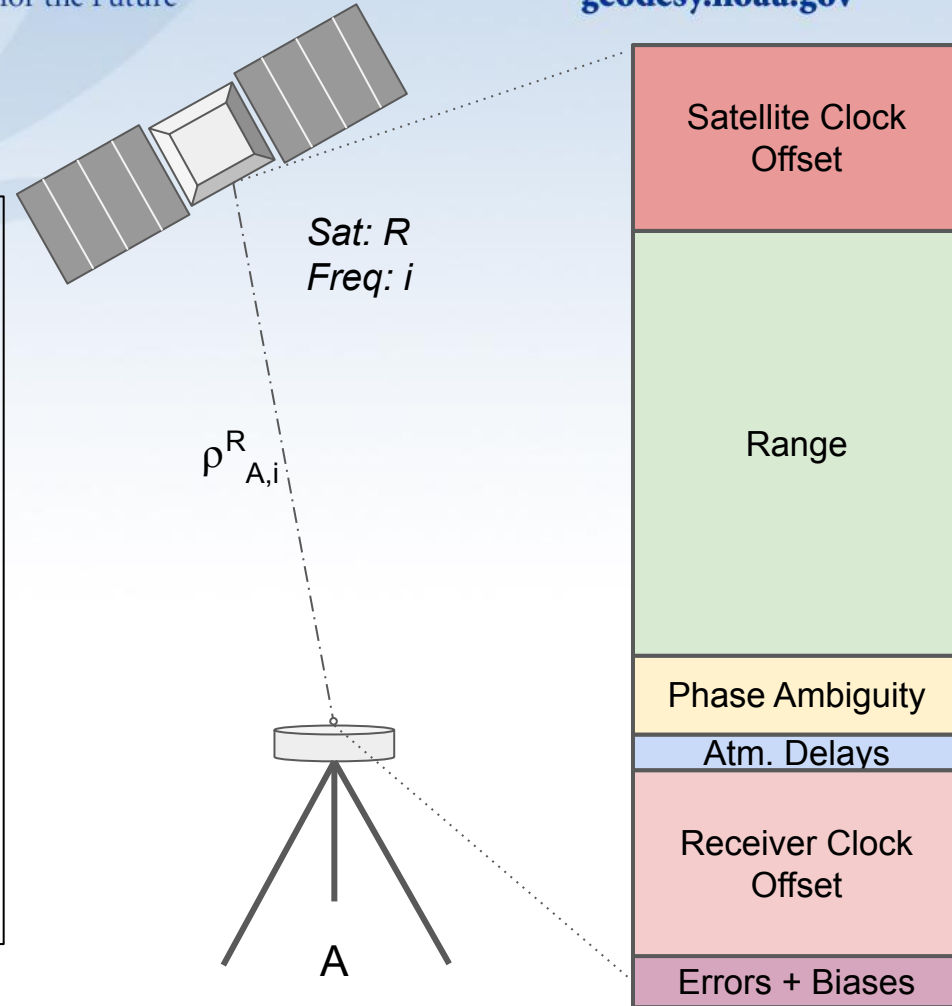


# GNSS Measurements

**Pseudorange** and **carrier phase** measurements are comprised of the following:

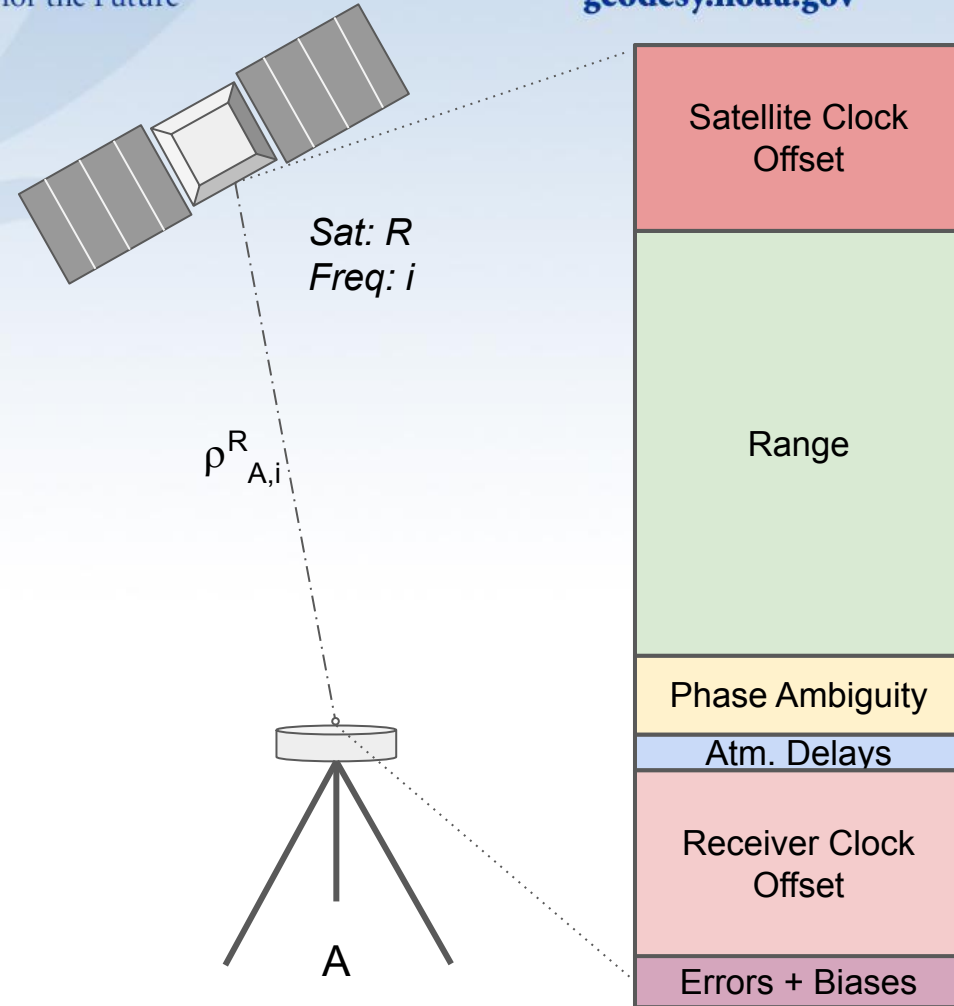
- Range = true satellite-receiver distance
- Satellite clock offset = satellite time offset relative to GPS system time
- Atmospheric delays = signal path delays through ionosphere and troposphere
- Receiver clocks offset = receiver time offset relative to GPS system time
- Carrier phase ambiguity (arbitrary integer value-phase only)
- Other errors = measurement errors, biases, etc.

We must estimate, model, or try to cancel out the error sources!

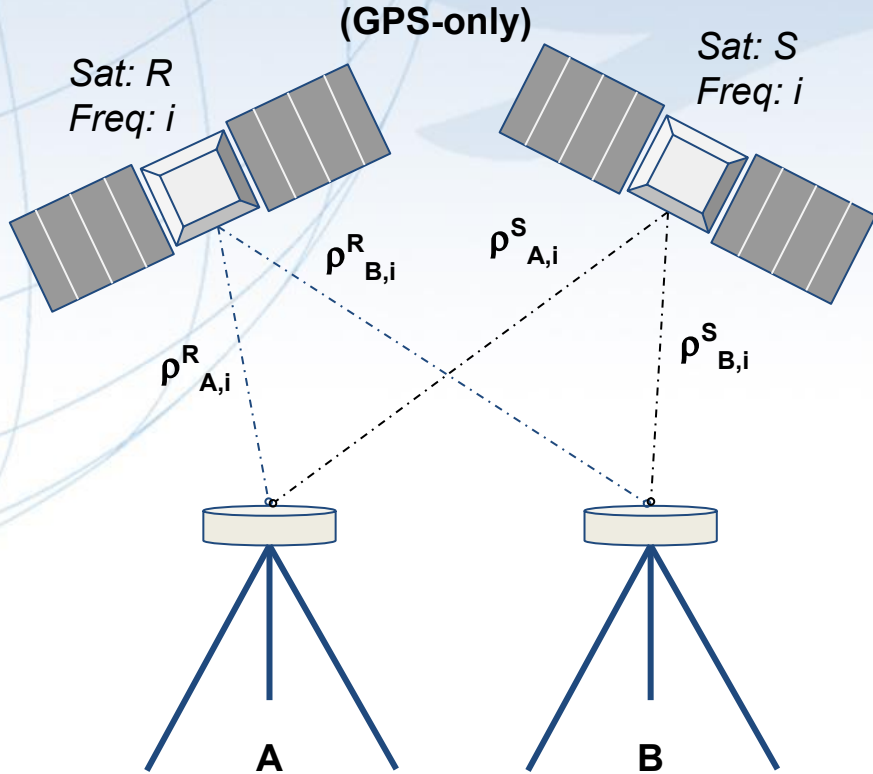


# Why not PPP?

- PPP = Precise Point Positioning
- PPP is an attractive alternative to baseline positioning; especially in regions where CORS coverage is sparse
- NGS operations rely heavily on GNSS vectors/network adjustments
- The M-PAGES software has been designed in a modular way to make future development easier

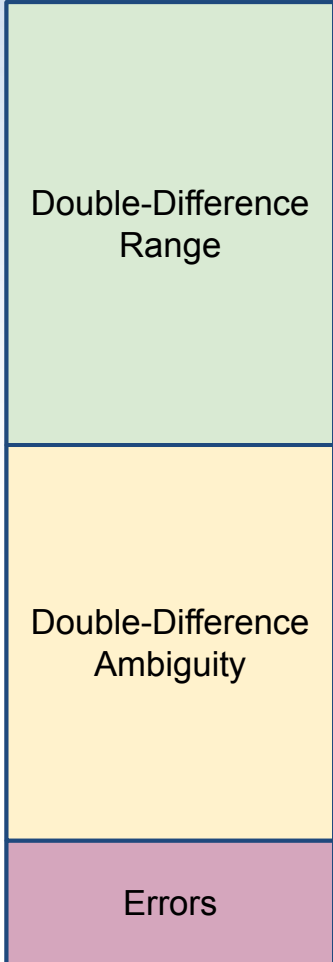


# Double-Difference Processing (PAGES)

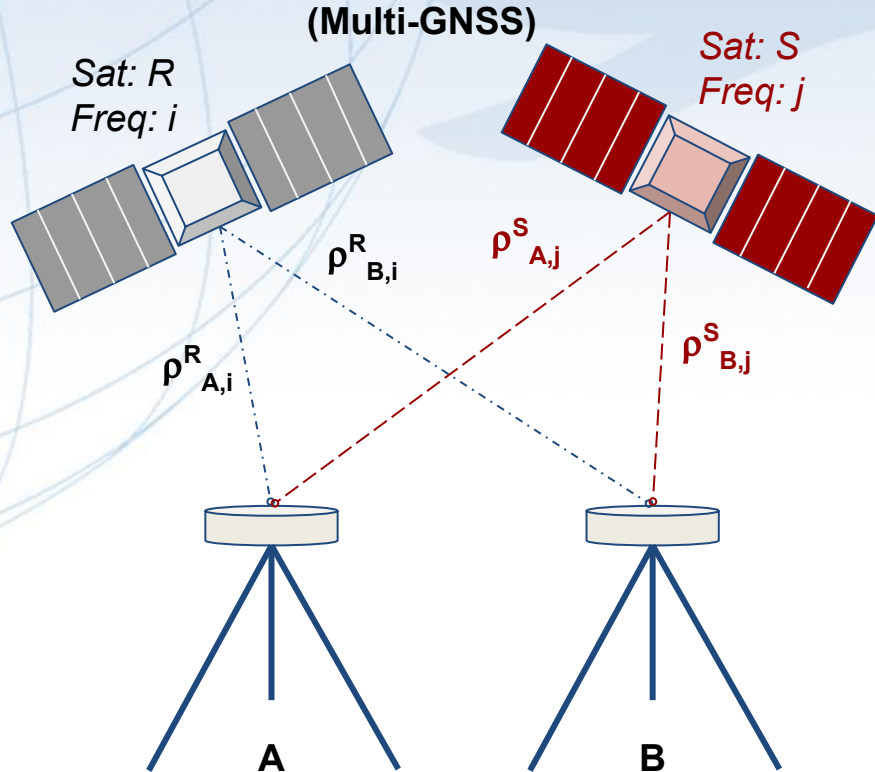


DD:  $\rho_{AB,i}^{RS} = SD^R - SD^S$

- Satellite **and** Receiver terms cancel
- For short baselines, atmospheric delays cancel
- Same frequencies for each satellite  $\rightarrow$  phase ambiguities can be resolved



# Why not double-difference?



DD:  $\rho^{RS}_{AB,i} = SD^R - SD^S$

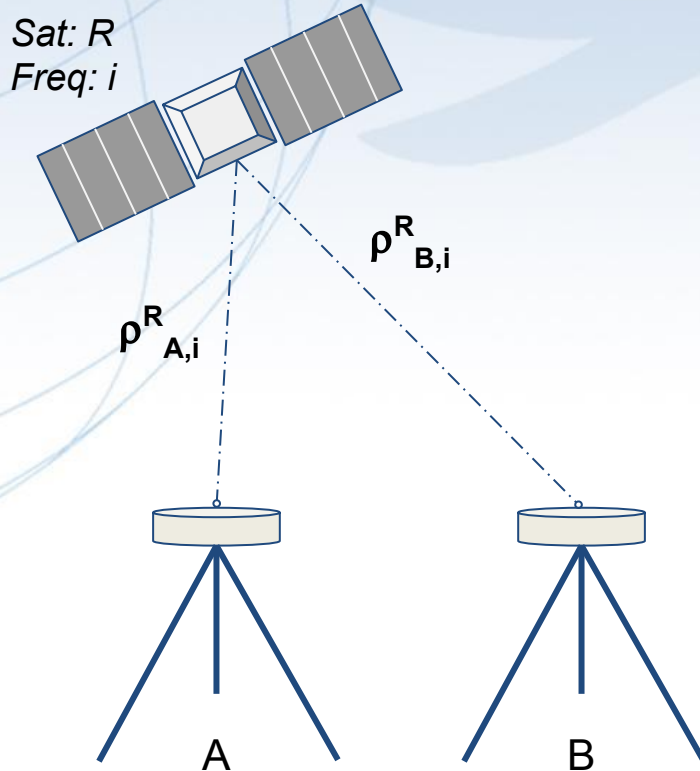
- Frequency  $i \neq j$
- Different frequencies prohibit ambiguity resolution!
- Could process each system separately then combine

Double-Difference Range

Double-Difference Ambiguity (float)

Errors + Biases

# Single-Difference Processing (M-PAGES)



$$SD^R: \quad \rho_{AB,i}^R = \rho_{A,i}^R - \rho_{B,i}^R$$

- Satellite-specific terms cancel
- Receiver clock terms do not cancel and must be estimated!
- Same frequencies for each satellite  $\rightarrow$  phase ambiguities can be resolved
- Flexible for multi-GNSS

Single-Difference Range

Single-Difference Ambiguity

Relative Receiver Clock Offset

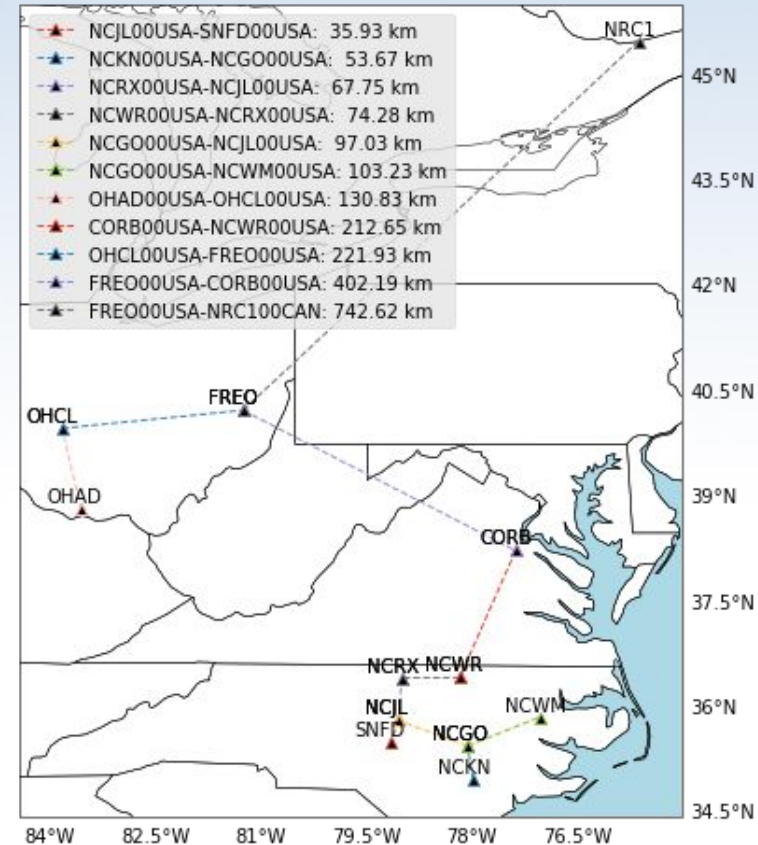
Errors + Biases

# M-PAGES Testing: CORS data

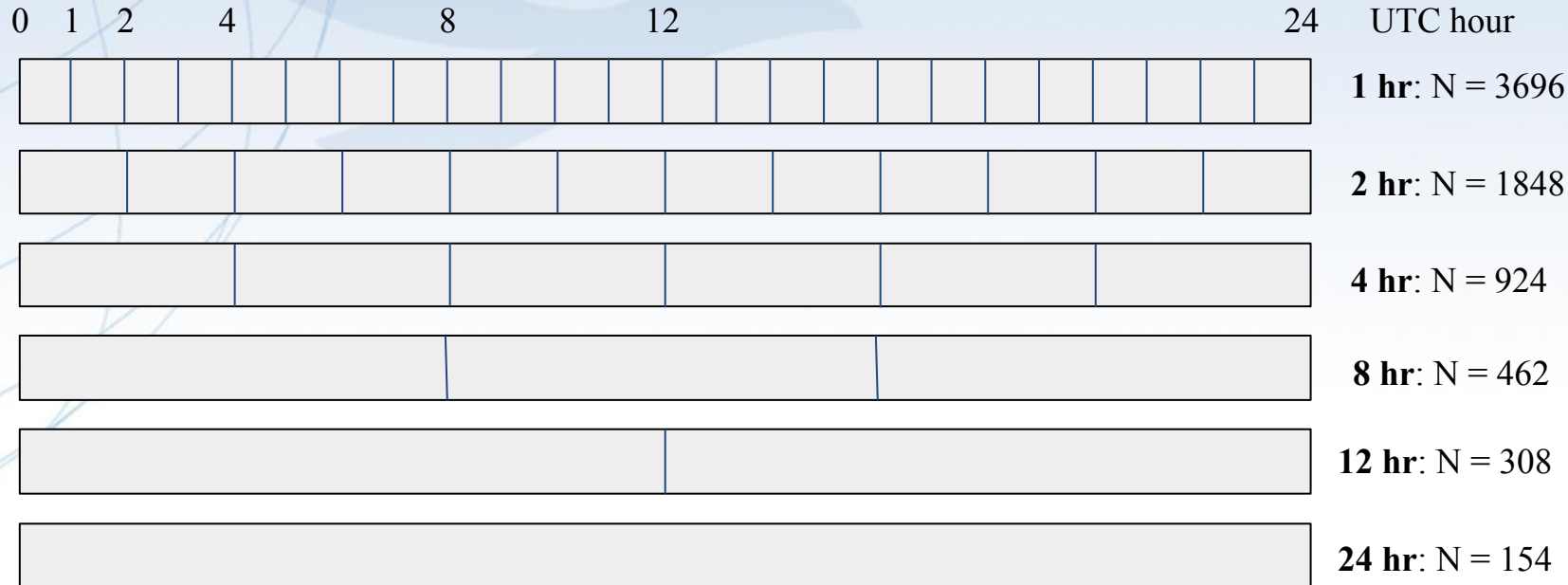


# Multi-GNSS CORS Tests

- 11 baselines picked from high quality CORSs
- Single baseline solutions
  - “Reference” CORS tightly constrained
  - “Rover” CORS coordinates estimated and compared to MYCS2 coordinate functions
- All stations track GPS+GLO+GAL (GRE)
- All possible sub-sessions processed for:
  - 14 consecutive days for each baseline (May 2022; doy 121-134)
  - Durations: 1, 2, 4, 8, 12, and 24 hours
  - G/GR/GE/GRE
- GLONASS (R) ambiguities = float

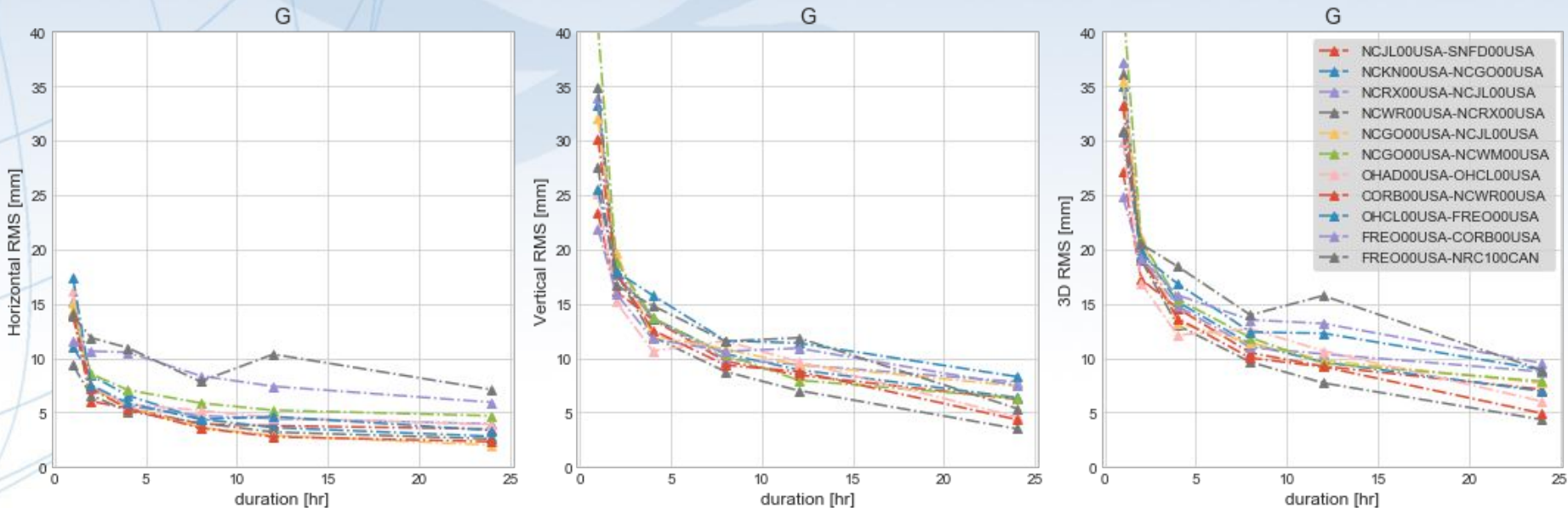


# Multi-GNSS CORS Tests



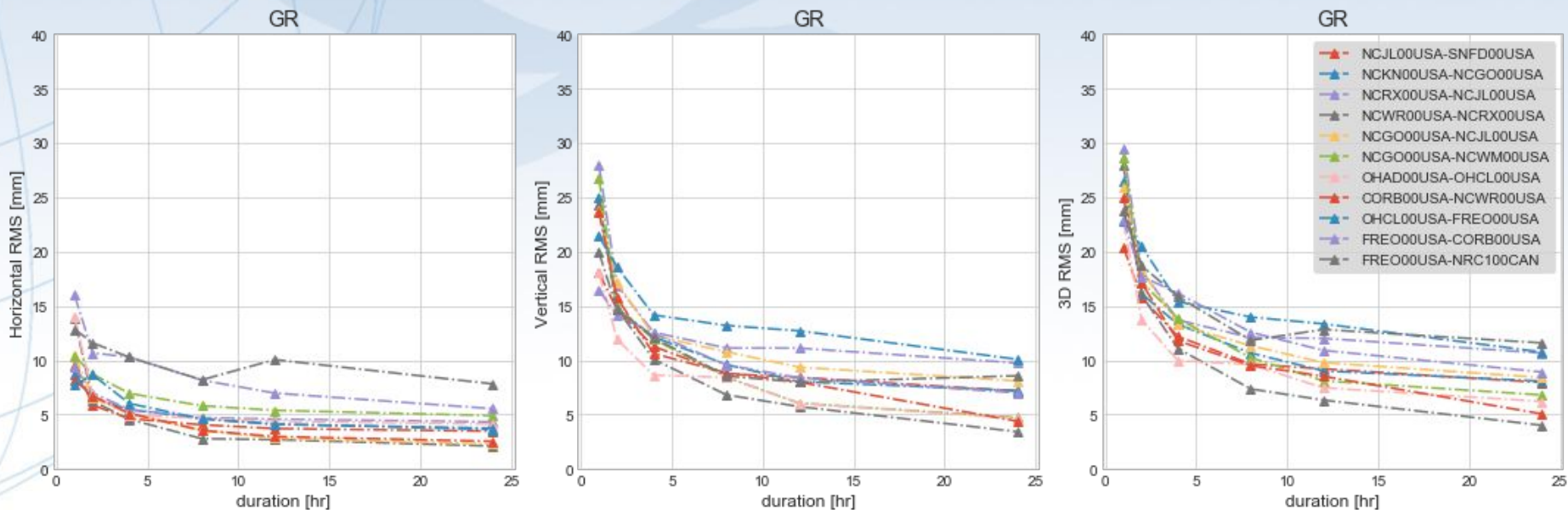
- Each 24 hour RINEX file (represented by a block) is divided into sub-sessions for each duration
- Total sessions (N) = (# of baselines) \* (# of days) \* (sessions per day)
  - Example: 24 hr → 11 \* 14 \* 1 = 154

# GPS



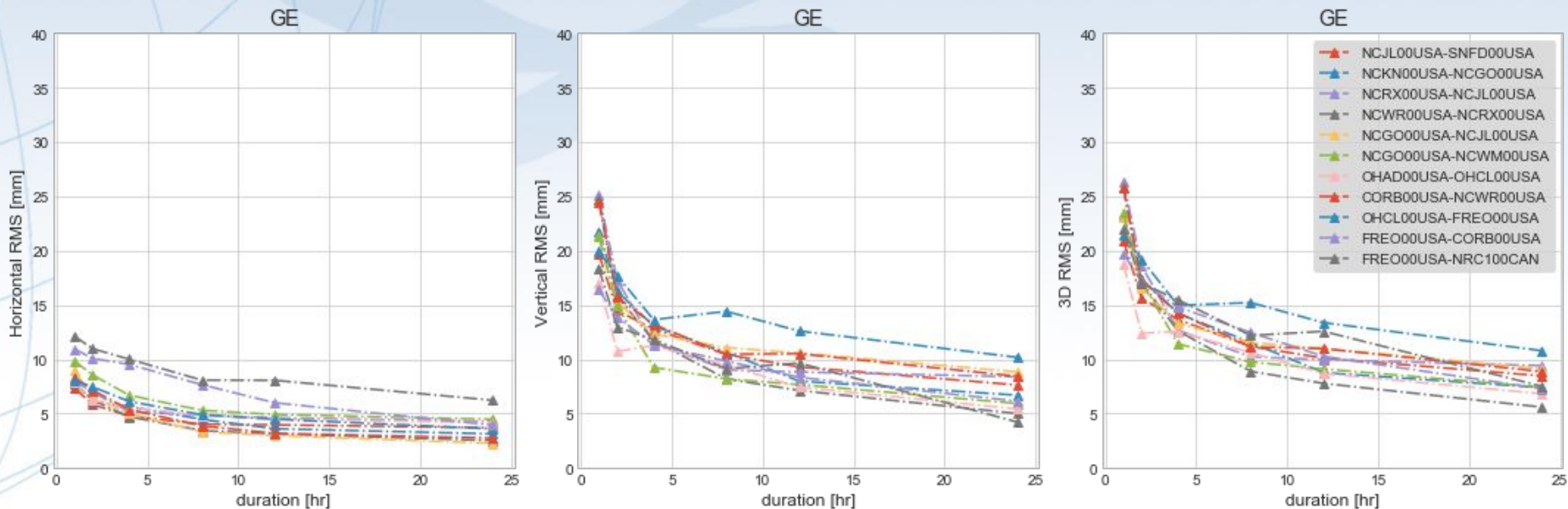
- RMS values computed per baseline and per session duration
- Large outliers removed using  $4 * \text{RMS}$  for each component

# GPS + GLO



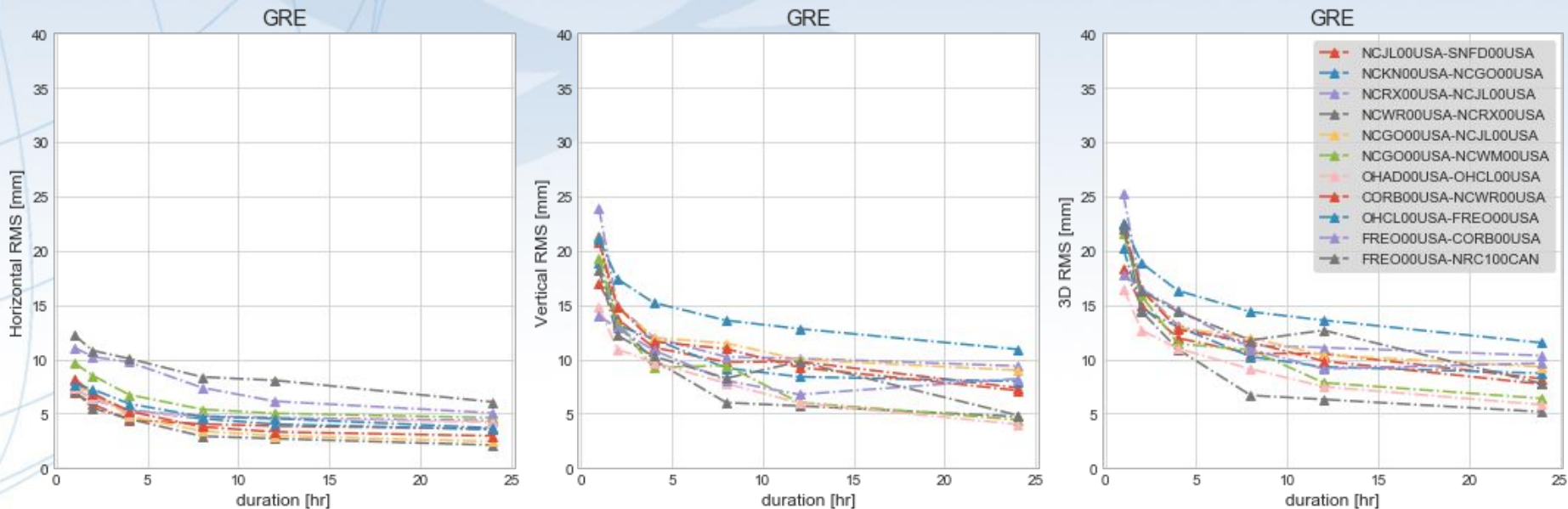
- RMS values computed per baseline and per session duration
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# GPS + GAL



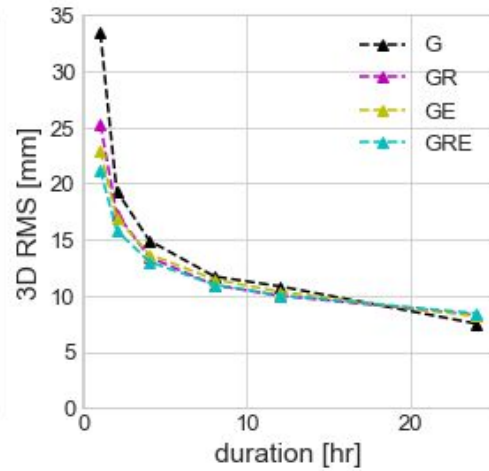
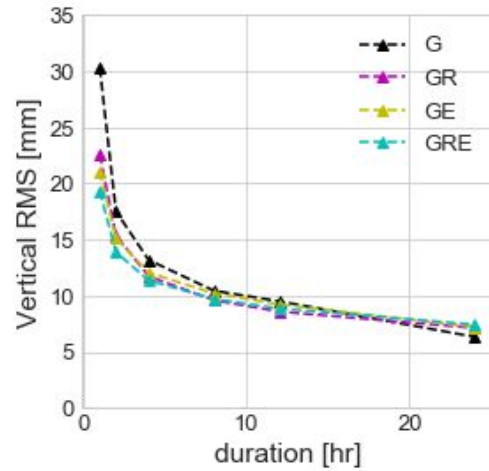
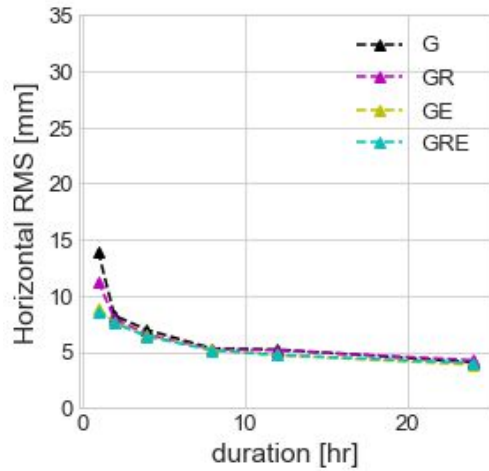
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# GPS + GLO + GAL



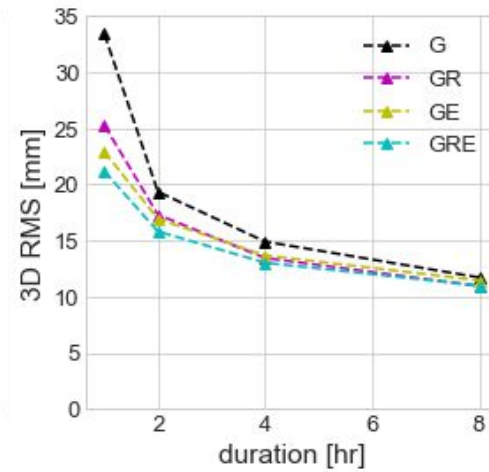
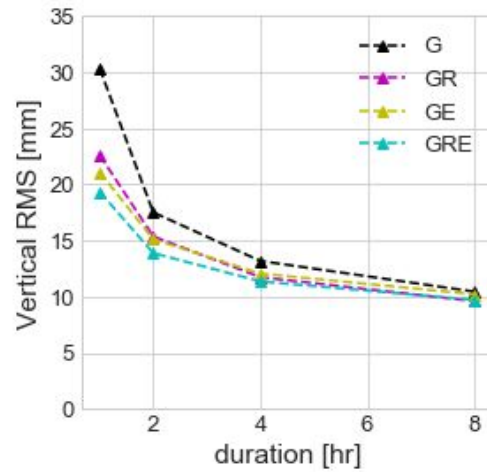
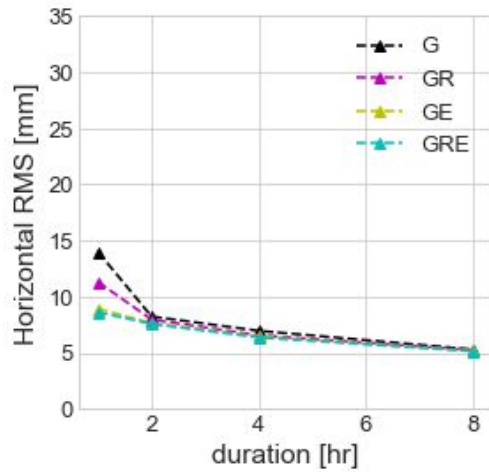
- RMS values computed per baseline and per session duration
- Large outliers removed using  $4 * \text{RMS}$  for each component





- RMS values for all baselines processed
- Significant improvements with added GNSS for shorter sessions
- Large outliers removed

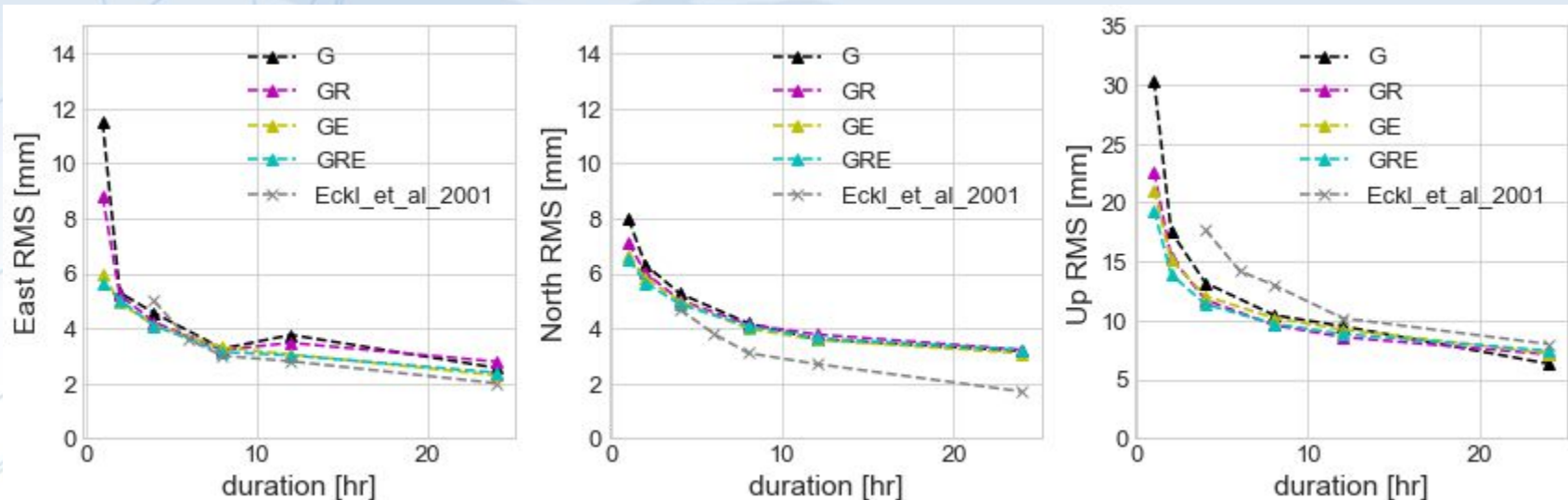
GNSS	Duration [hr]	Percent Improvement (wrt GPS-only)		
		HRMS	VRMS	3D
GR	1	19.2	25.5	24.3
	2	3.4	12.2	10.6
	4	5.7	11.0	9.8
	8	1.2	8.1	6.7
GE	1	36.1	30.5	31.4
	2	7.4	13.7	12.5
	4	7.2	8.6	8.3
	8	2.3	2.3	2.3
GRE	1	38.4	36.2	36.6
	2	8.1	20.7	18.3
	4	8.5	13.8	12.6
	8	2.9	7.0	6.2



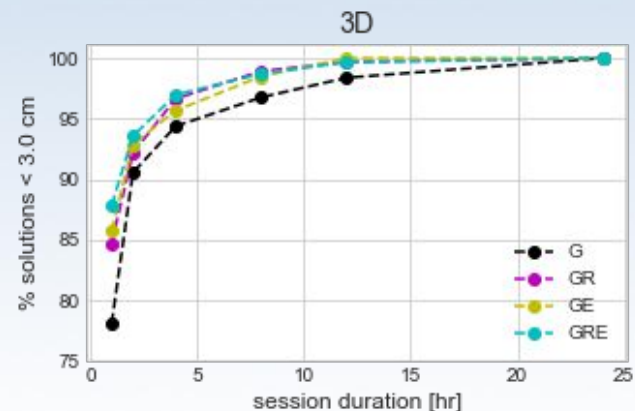
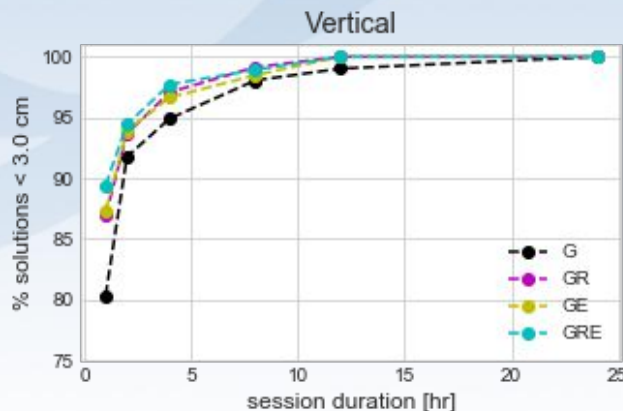
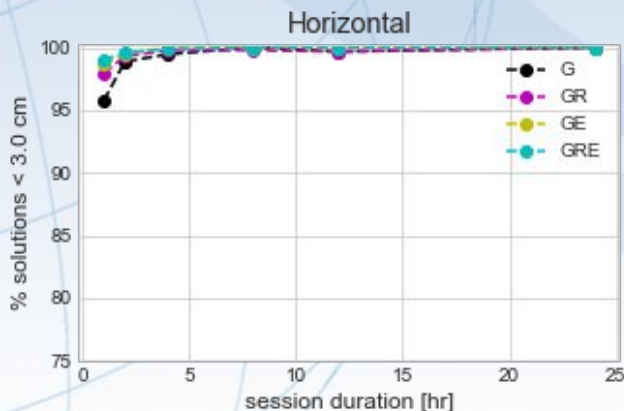
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	2	7.4	13.7	12.5
	4	7.2	8.6	8.3
	8	2.3	2.3	2.3
GRE	1	38.4	36.2	36.6
	2	8.1	20.7	18.3
	4	8.5	13.8	12.6
	8	2.9	7.0	6.2

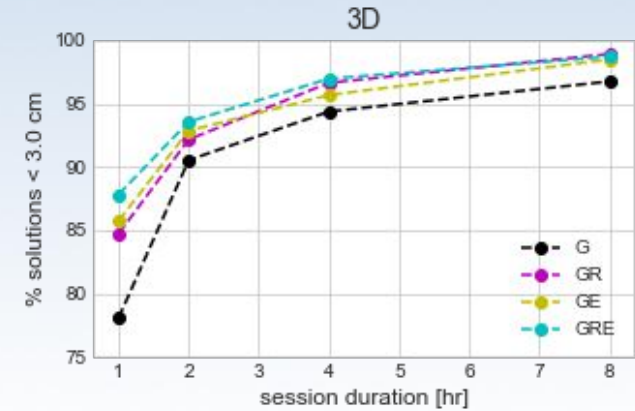
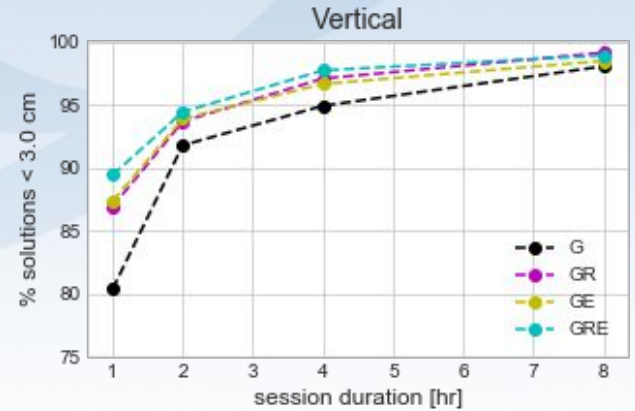
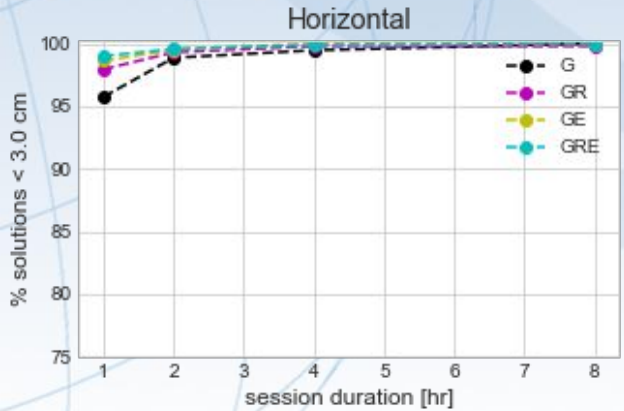
# So how does this compare to PAGES?



- Eckl et al. (2001) performed a similar study using PAGES
- Imperfect comparison due to difference time window and baseline selection
- M-PAGES results are quite consistent!



- Plots show percentage of solutions that agree with MYCS2 coordinates at 3 cm level (including outliers)
- Notable improvements for G→GRE solutions for shorter sessions



(Zoomed in on 1-8 hours)

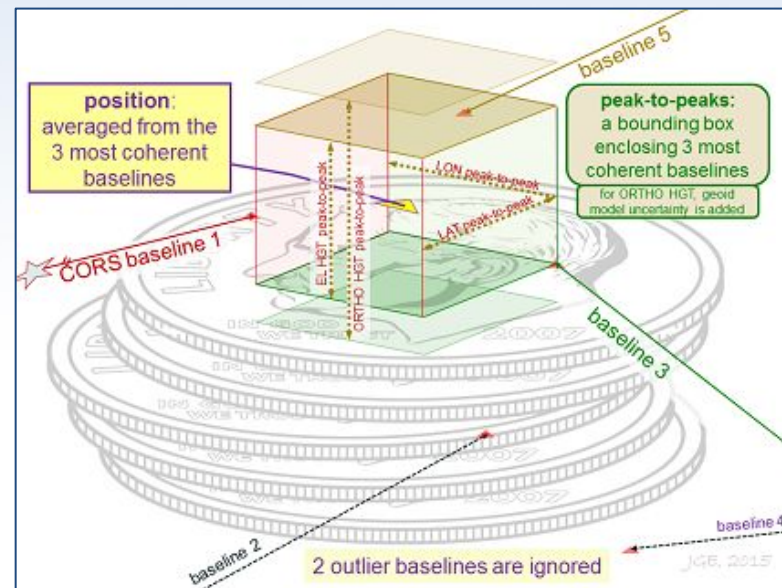
- Plots show percentage of solutions that agree with MYCS2 coordinates at 3 cm level (including outliers)
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# M-PAGES Testing: OPUS data



# OPUS-Static

- User submits a rover RINEX file along with antenna height/type
- Five single baseline solutions are processed to nearby CORS
- OPUS-S solution = average of best three baseline solutions
- OPUS-S uncertainties = peak to peak errors of best three (right)



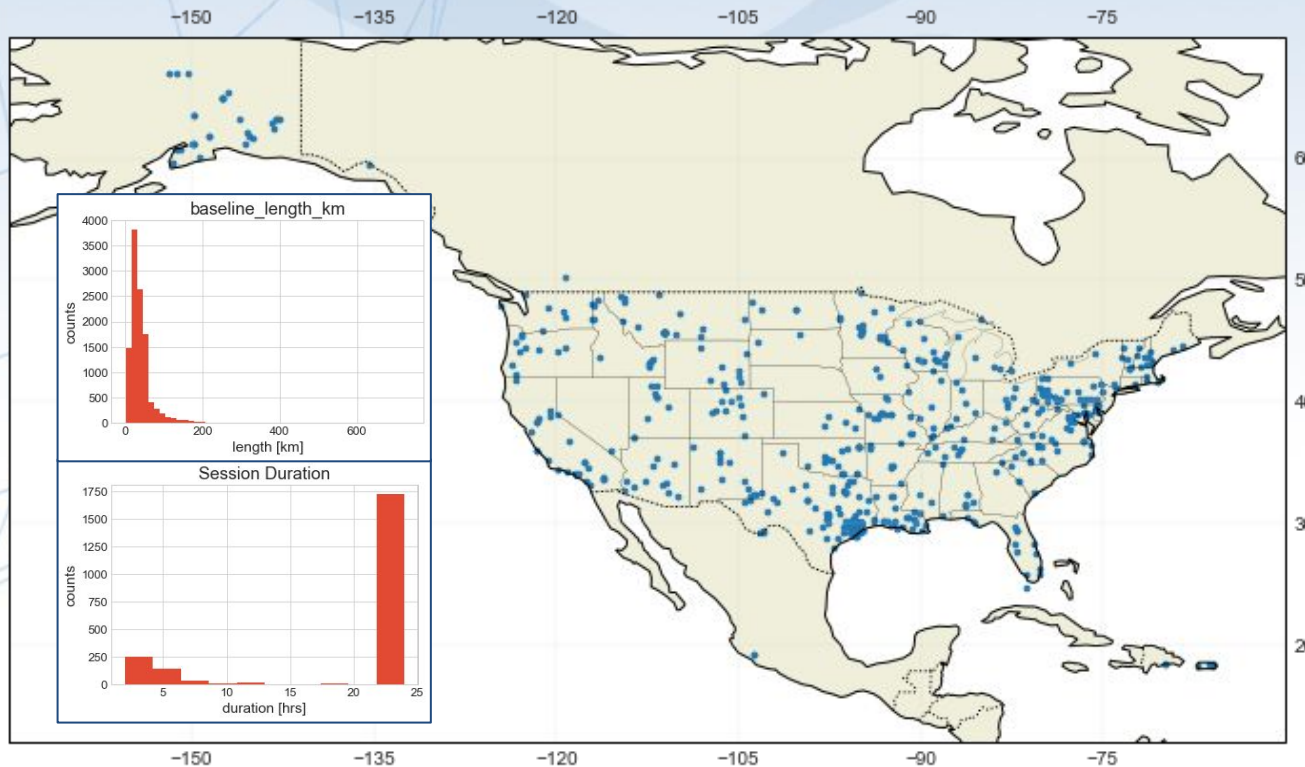
<https://geodesy.noaa.gov/OPUS/about.jsp>

# OPUS-S Testing

- For a selection of ~2500 OPUS submissions:
  - Process each of the 5 baselines with M-PAGES (**GPS only**)
  - Compare each single-baseline solution with the corresponding PAGES solution
  - Compare the OPUS-S solution for M-PAGES with PAGES
    - i.e., Average of the best three baselines

The screenshot shows the OPUS: Online Positioning User Service website. The header includes the NOAA logo and the text "OPUS: Online Positioning User Service" and "National Geodetic Survey". A navigation bar contains links for "NGS Home", "About NGS", "Data & Imagery", "Tools", "Surveys", and "Science & Education", along with a search box. The main content area features a "Sept 2021: BETA OPUS projects released! Please provide your feedback" announcement, a "Upload your data file." section with a "Choose File" button and a "NONE" dropdown menu, and a "What is OPUS? FAQs" section. A sidebar on the left contains an "OPUS menu" with links for "home / upload about OPUS", "projects", "shared solutions", "planned improvements", and "support / feedback". The bottom of the page has buttons for "Upload to Rapid-Static" and "Upload to Static" with their respective data processing times.

<https://geodesy.noaa.gov/OPUS/>



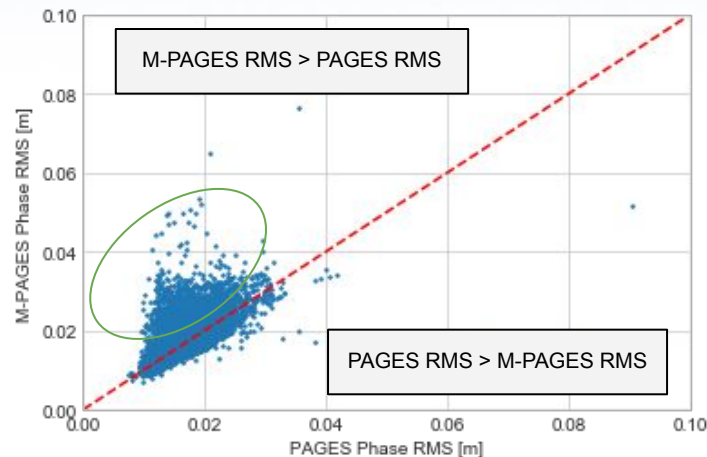
- The majority of data processed:
  - < 200 km baselines
  - 24 hour sessions
- Large quantity of submissions in Texas

# Consistency of individual baseline solutions

- Percentage\* of solutions that PAGES and M-PAGES solutions agree within threshold
- Population of solutions with higher RMS for M-PAGES (Bottom right; Green oval)
- Room for improvement!

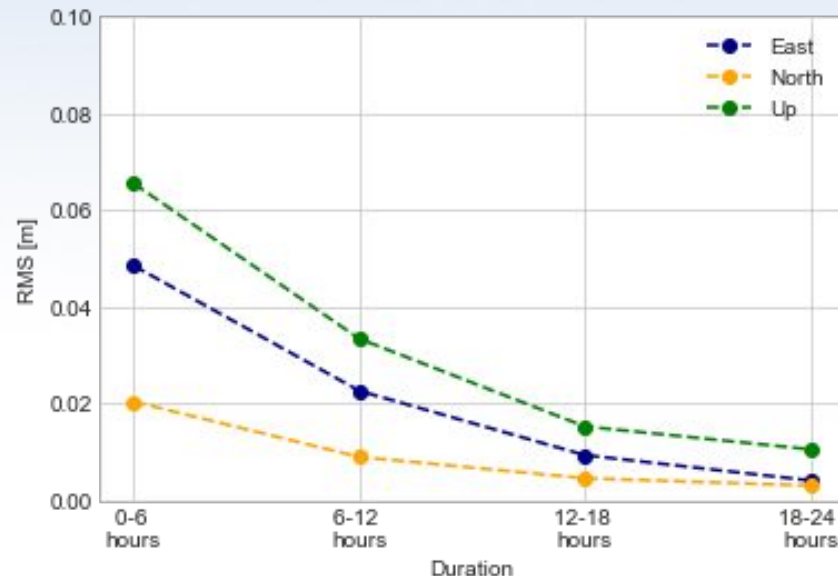
\* Total baseline solutions = 12430

Component < 3 cm	N	%
Horizontal	11792	95.55
Vertical	11711	94.90
3D	11029	89.37



# Consistency of individual baseline solutions

- RMS of coordinate differences between M-PAGES and PAGES
- Values averaged for sessions grouped by duration with large outliers removed





# Consistency of OPUS-S solutions

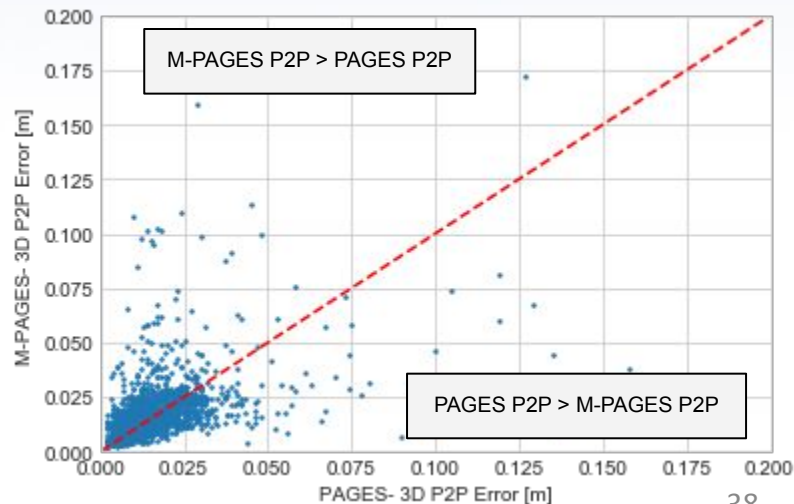
- (1) Percentage\* of solutions that M-PAGES/PAGES OPUS-S coordinates agree below threshold
  - OPUS-S coordinates = average of best three baseline solutions
- (2) Percentage\* of solutions with peak to peak (P2P) error magnitude < threshold
  - Each software package yields solutions with large P2P error (see figure)

\*Total solutions = 2471

(1) Component < 3 cm	N	%
=====		
Horizontal	2371	95.95
Vertical	2388	96.64
3D	2281	92.31

(2) P2P < 3 cm	N	%
=====		
M-PAGES	2296	92.92
PAGES	2302	93.16





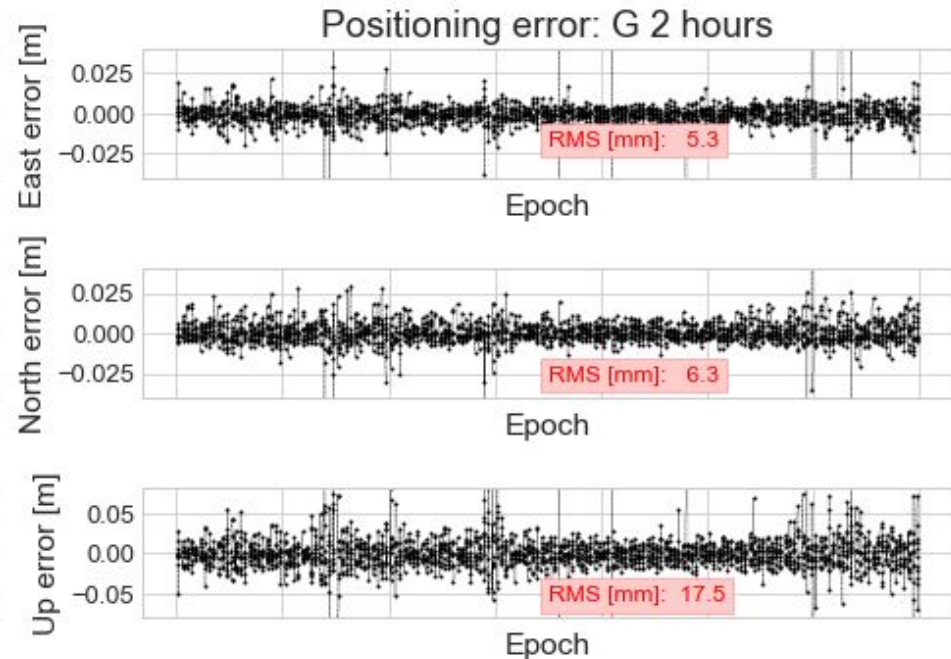
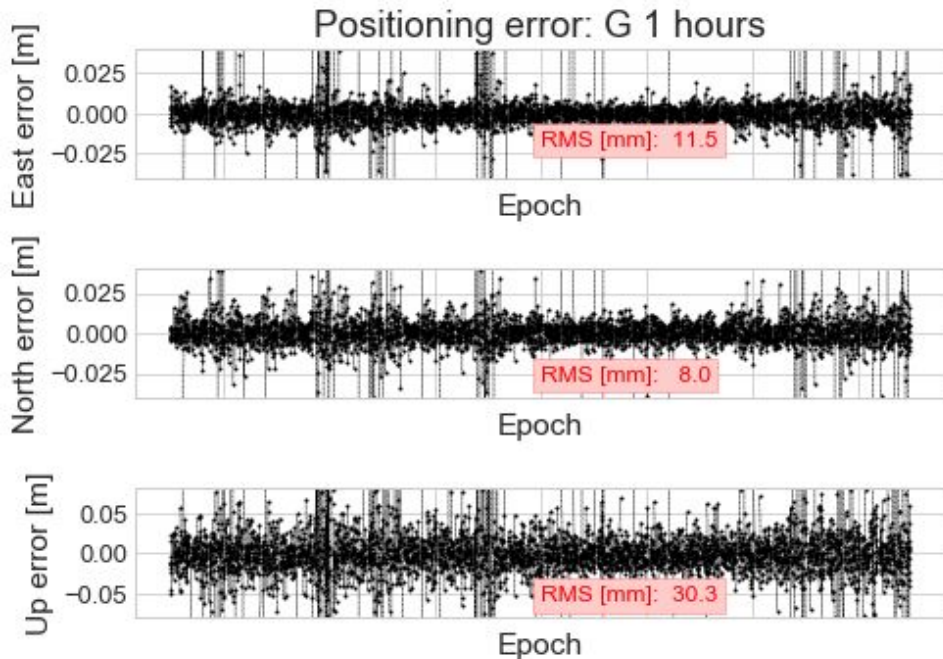
# Looking Ahead

- Planned integration of M-PAGES in Beta OPUS-S by end of calendar year (2022)
  - Once released, please test and provide feedback!
- Future OPUS User Forum will provide more detail about M-PAGES integration- stay tuned!
- Ongoing R&D:
  - Improved ambiguity resolution, cycle slip/outlier detection
  - Testing, testing, testing
  - Prep for integration into OPUS-Projects and GNSS orbit determination

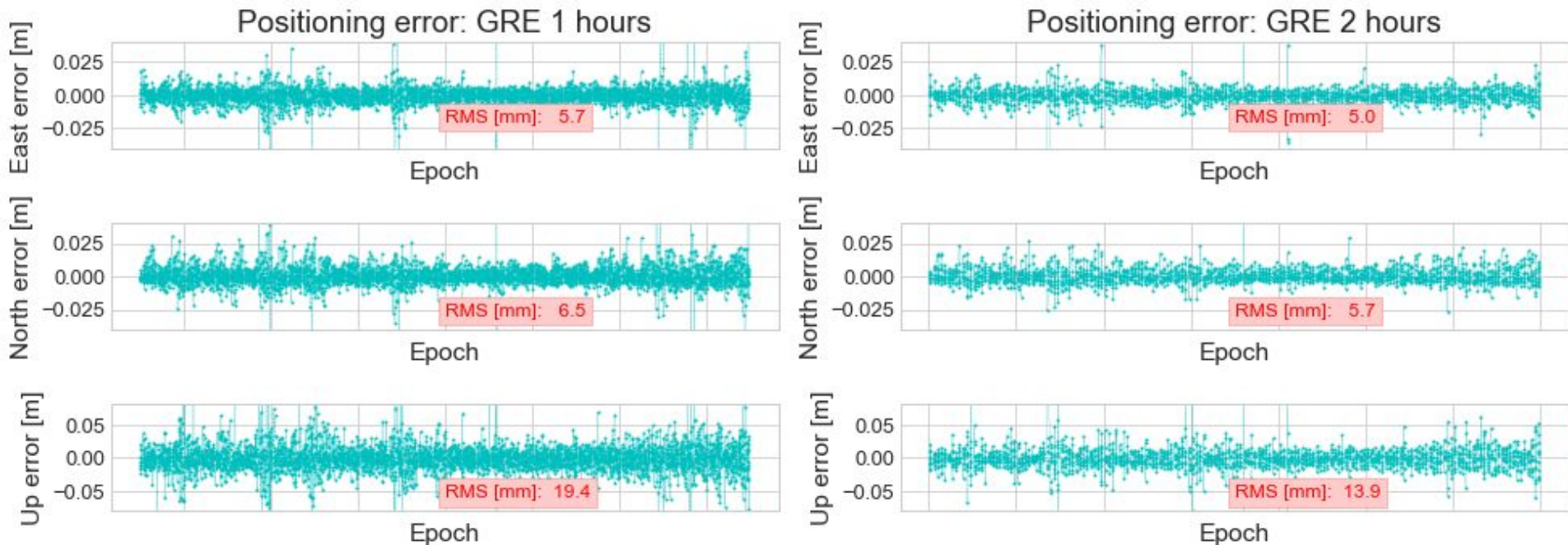
# Key Points

- M-PAGES is capable of processing GNSS data for all dual-frequency systems
- Improved positioning with multi-GNSS data can be demonstrated with M-PAGES
- M-PAGES is still under active development, but OPUS-S integration is underway

# Extra Slides



- X-axes: mean epoch of each session
- Y-axes: positioning errors wrt MYCS2 coordinates for all baselines
- Outliers are included in these plots



- X-axes: mean epoch of each session
- Y-axes: positioning errors wrt MYCS2 coordinates for all baselines
- Outliers are included in these plots
- **Notable improvements and fewer outliers with GLO+GAL added!**